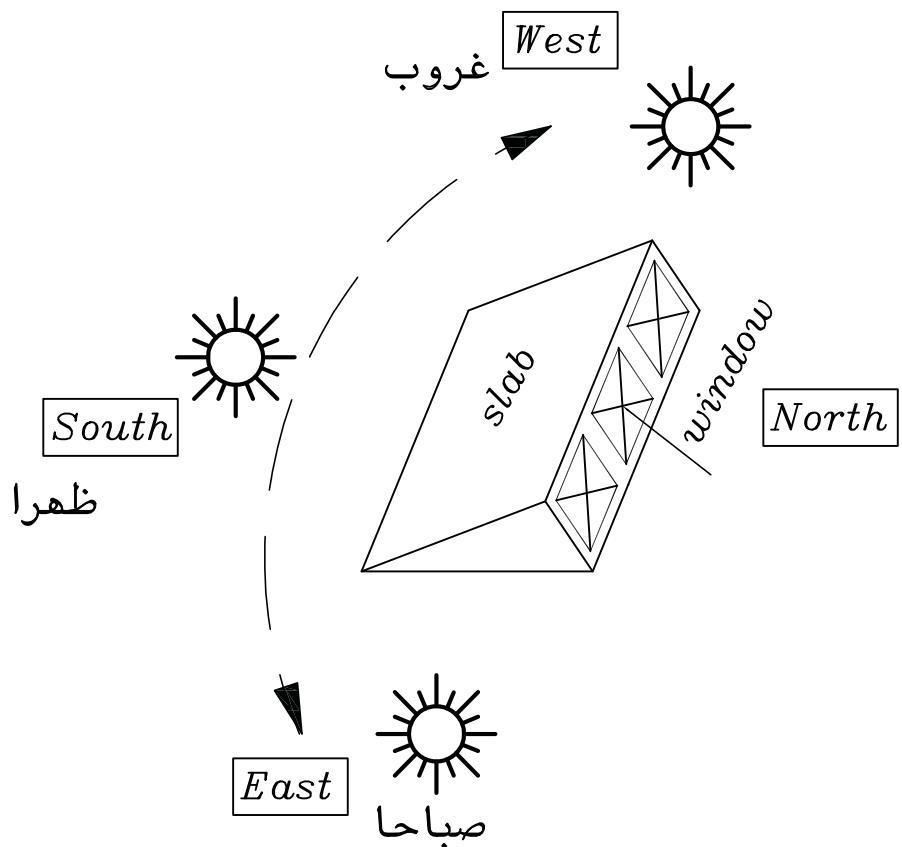


# Saw Tooth Structures

## (North Light Structures)

منشآت يشترط فيها عدم تعرضاً لضوء الشمس المباشر وذلك نظراً لأن الضوء المباشر يمكن أن يسبب أضرار داخل المنشأ مثل مصانع المنسوجات والبويات والمواد الملتهبة.



من الشكل الموضح نجد أن الشباك لا يرى الشمس مطلقاً في اي فترة من فترات النهار وبالتالي تكون الاضاءة غير مباشرة كذلك تكون النوافذ في اتجاه التهوية (الاتجاه البحري).

### Types of Saw Tooth Structures

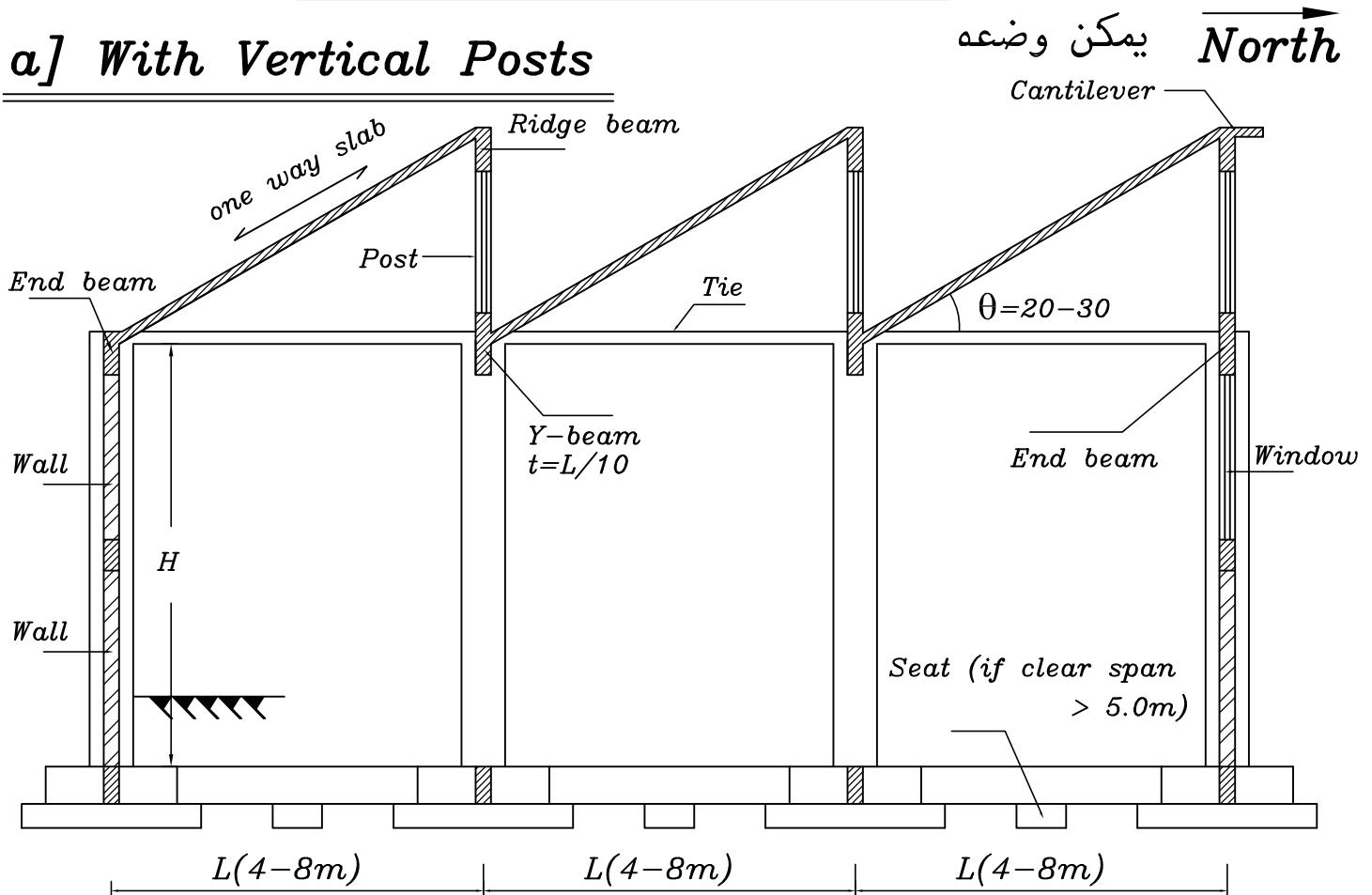
1] Slab Type  $4 \rightarrow 8m$

2] Girder Type  $8 \rightarrow 12m$

3] Saw tooth Supported on a system [ frame, Polygon, Arch girder, Truss ]

# 1] Saw Tooth Slab Type

## a] With Vertical Posts



Saw Tooth Slab Type is used for Span (4-8m)

### Concrete Dimensions

-One way Solid Slab (4  $\rightarrow$  5m)

-One way H.B. Slab (5  $\rightarrow$  8m)

-Tie (300\*300)

-Post (250\*250)

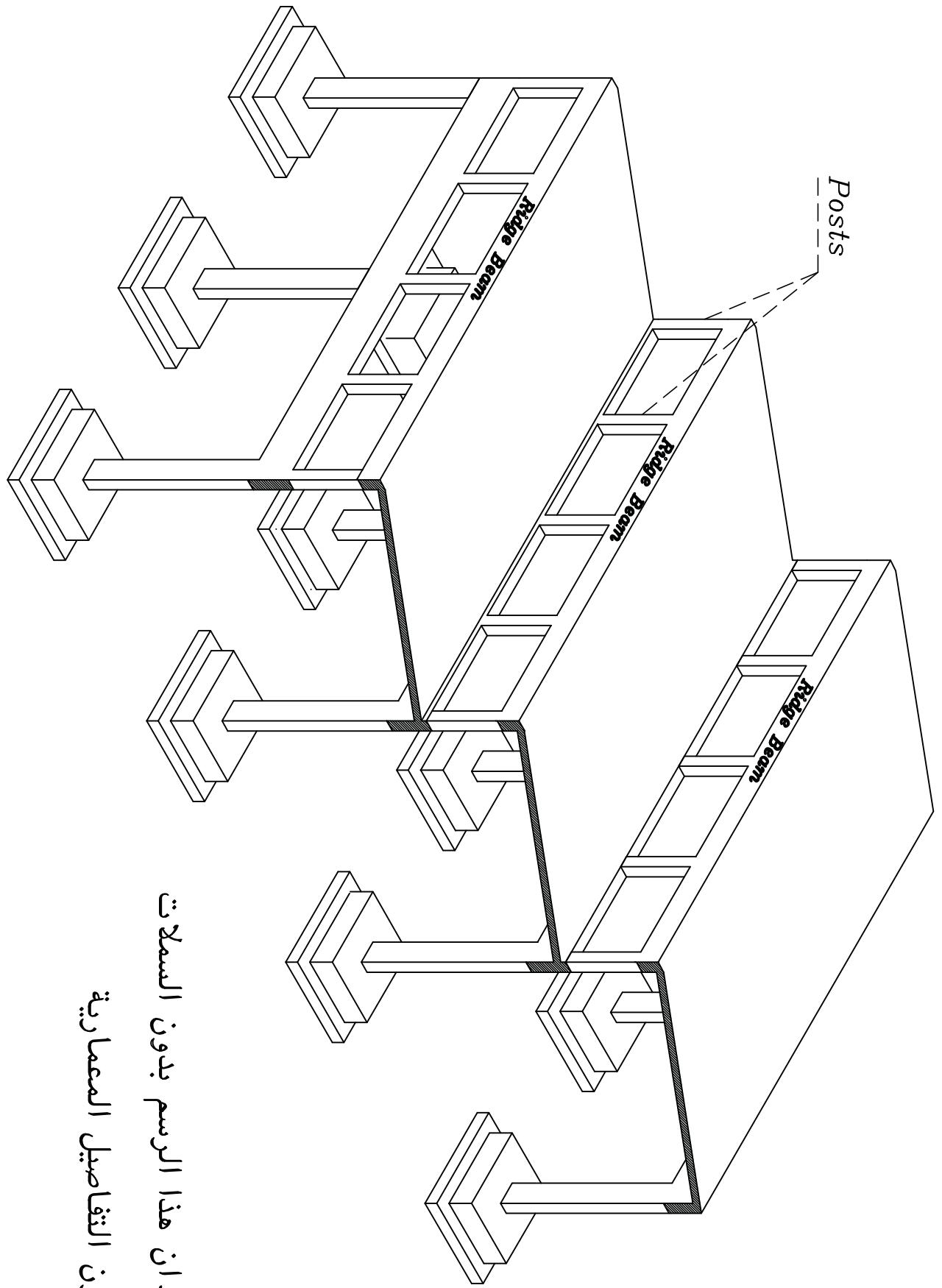
-Distance between posts (2  $\rightarrow$  3m)

$$- t(\text{col}) = \frac{H}{12}$$

- ملحوظة

يتم وضع Tie للتربيط بين الاعمدة فقط.  
ويمكن عدم وضعه

# حاول ان تتخيل عناصر ال System

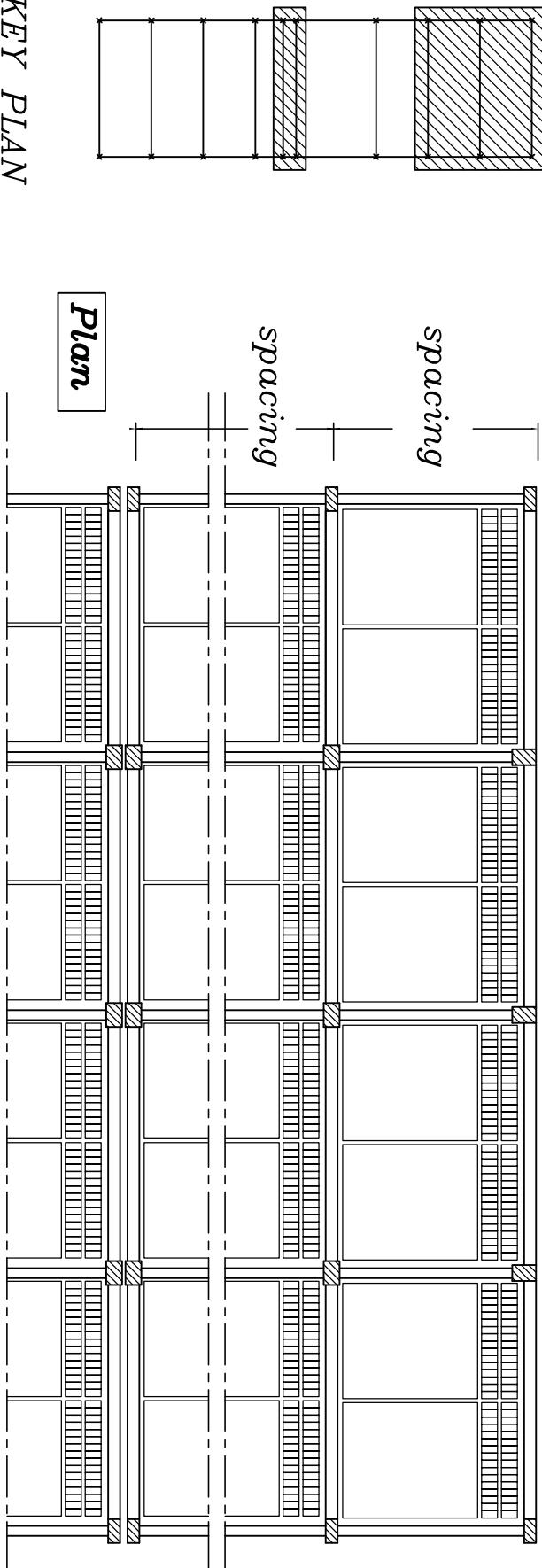


لا حظ ان هذا الرسم بدون السملات  
و بدون التفاصيل المعمارية

By Eng. Ezz El-Din Mostafa & Eng. Yasser M. Samir

1:2000 → 1:400

## KEY PLAN



By Eng. Ezz El-Din Mostafa & Eng. Yasser M. Samir

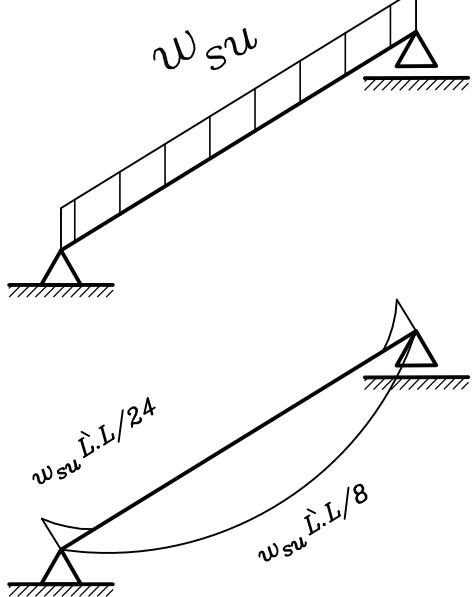
Architectural floor plan of a building. The plan shows a central entrance with a double door, flanked by two rectangular rooms. To the right of the entrance is a large rectangular room. To the left is a smaller rectangular room. Further left, a staircase leads down. The plan is labeled with 'spacing' and 'L(4-8m)'.

## Steps of design

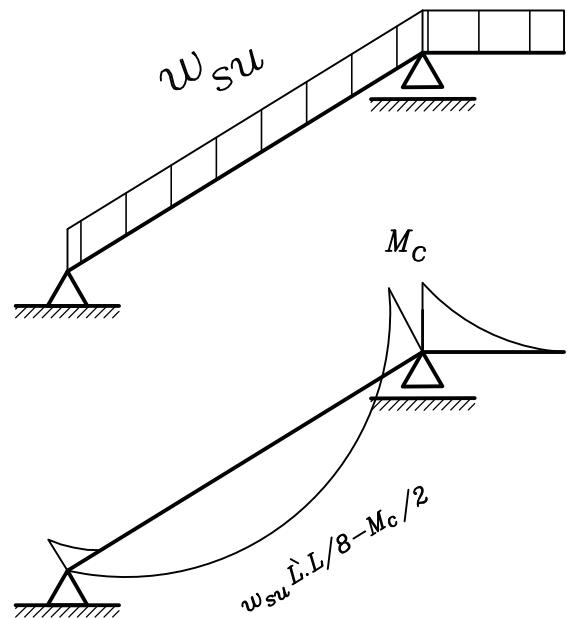
### 1] Analysis of Slabs

$$w_{su} = 1.4[t_s \gamma_c + F.C.] + 1.6L.L. \cos \theta \quad (\text{for S.S.})$$

$$w_{su} = \frac{1.4[t_s \gamma_c * (e+b) + b h \gamma_c + 5 * \text{wt. of block}]}{(e+b)} + 1.4F.C. + 1.6L.L. \cos \theta \quad (\text{for H.B.})$$



no cantilever

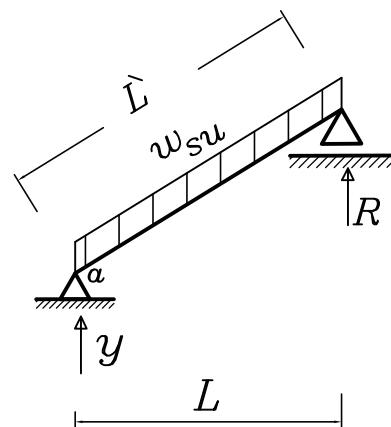


Case of cantilever

### 2] Reactions of slabs on beams

$$R = y = w_{su} \frac{L}{2} \quad kN/m$$

$h$



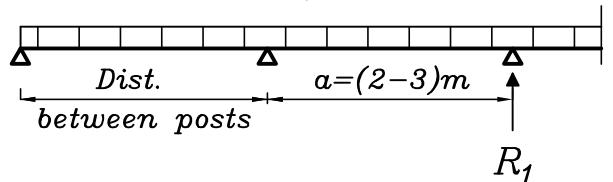
### 3]Analysis of Ridge beam(250\*400)

$$w = R + o.w$$

$$kN/m$$

$$R_1 = w * a$$

$$w \text{ kN/m'}$$



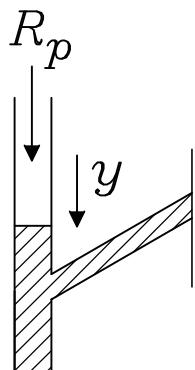
### 4]Design of Posts

$$R_p = R_1 + o.w \text{ of Post}$$

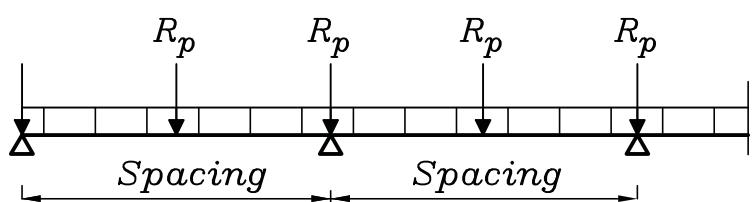
$$R_p = 0.35A_c f_{cu} + 0.67A_s f_y \rightarrow \text{get } A_s$$

### 5]Design of Y-beam

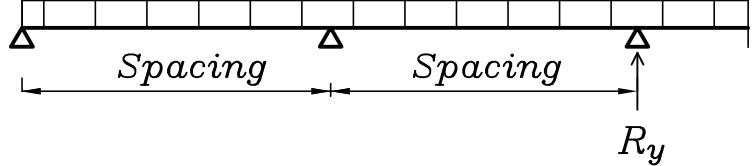
$$w_y = o.w + y + \frac{\Sigma R_p}{Span} \text{ kN/m}$$



$$R_y = w_y * \text{Spacing}$$



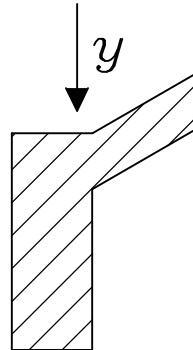
$$w_y \text{ kN/m'}$$



## 6]Analysis of End beam

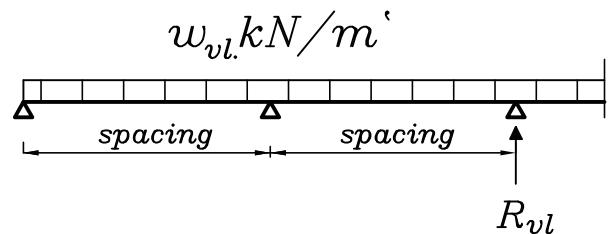
$$w_{vl.} = o.w + y$$

$$kN/m$$



$$R_{vl} = w_{vl} * Spacing$$

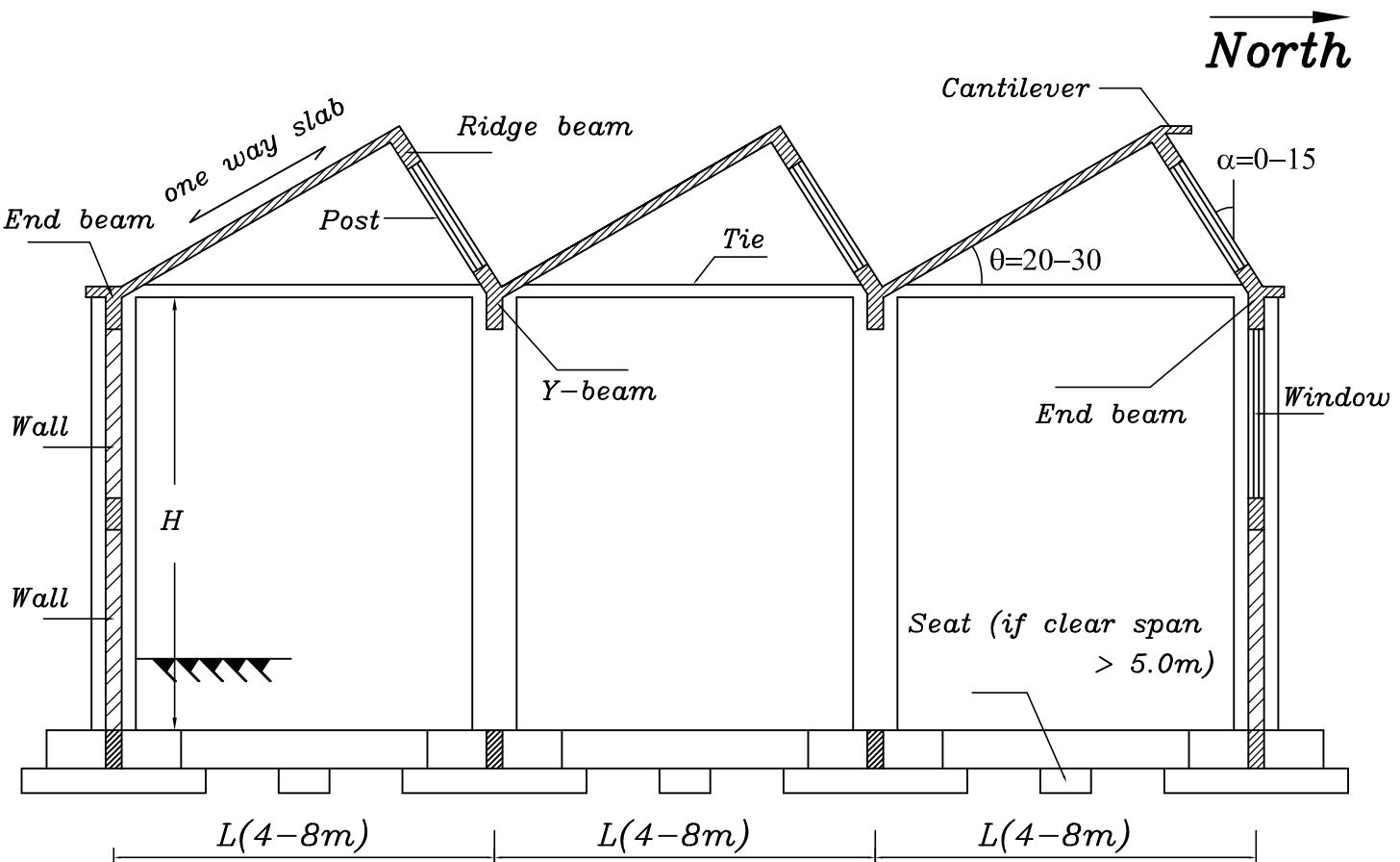
## 8]Design of Col.



$$P_{col.} = R_{y-beam}$$

Design  $N, M_{add.}$

## b]With Inclined Posts

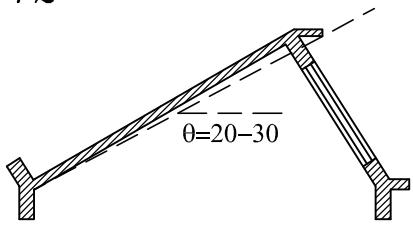


Saw Tooth Slab Type is used for Span (4-8m)

### Concrete Dimensions

- One way Solid Slab (4  $\rightarrow$  5m)
- One way H.B. Slab (5  $\rightarrow$  8m)
- Tie (b\*b)
- Post (250\*250)
- Distance between posts (2  $\rightarrow$  3m)
- $t(\text{col}) = \frac{H}{12}$

### ـ فائدة الكابولي

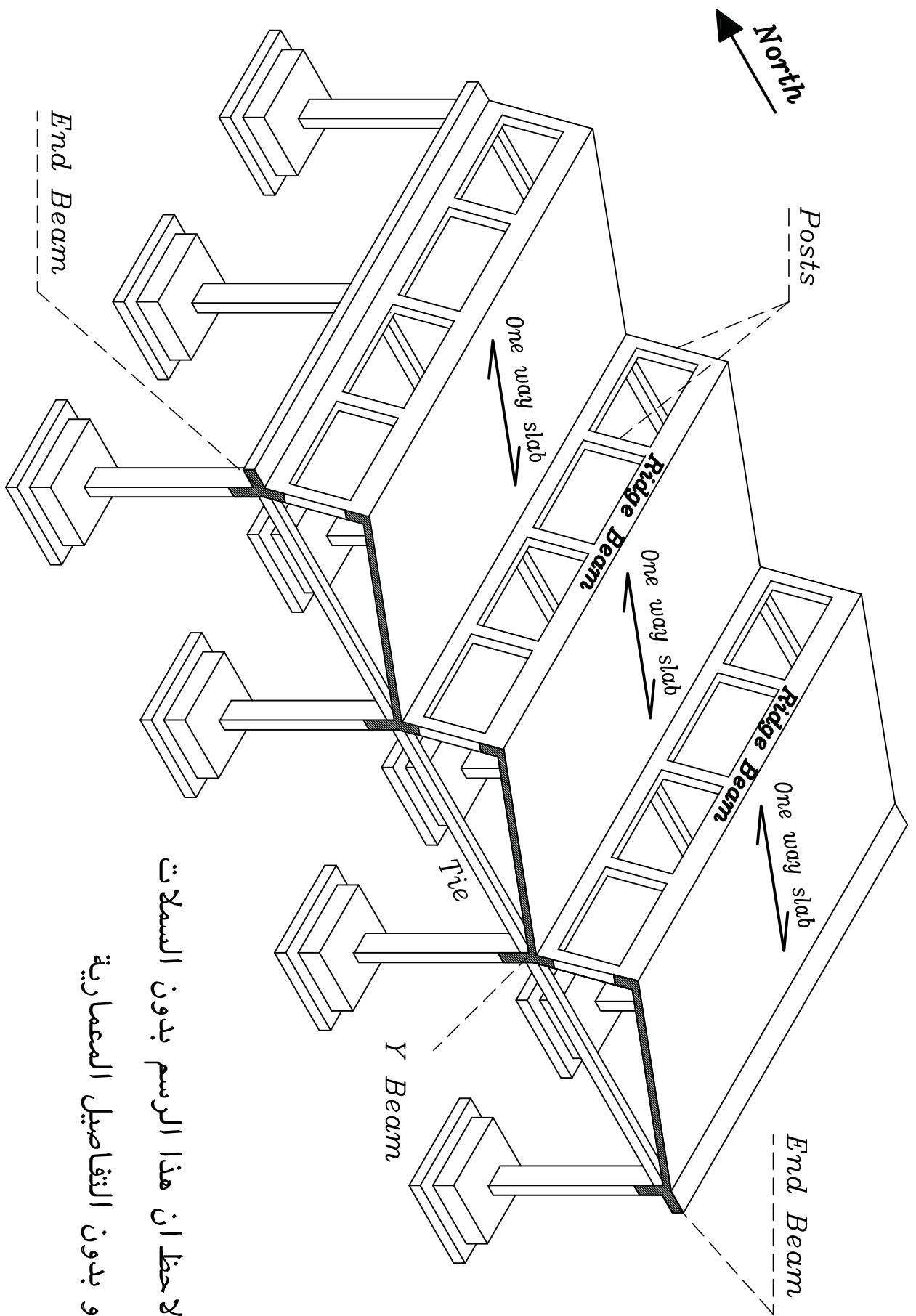


١ - تقليل زاوية الاضاءة .

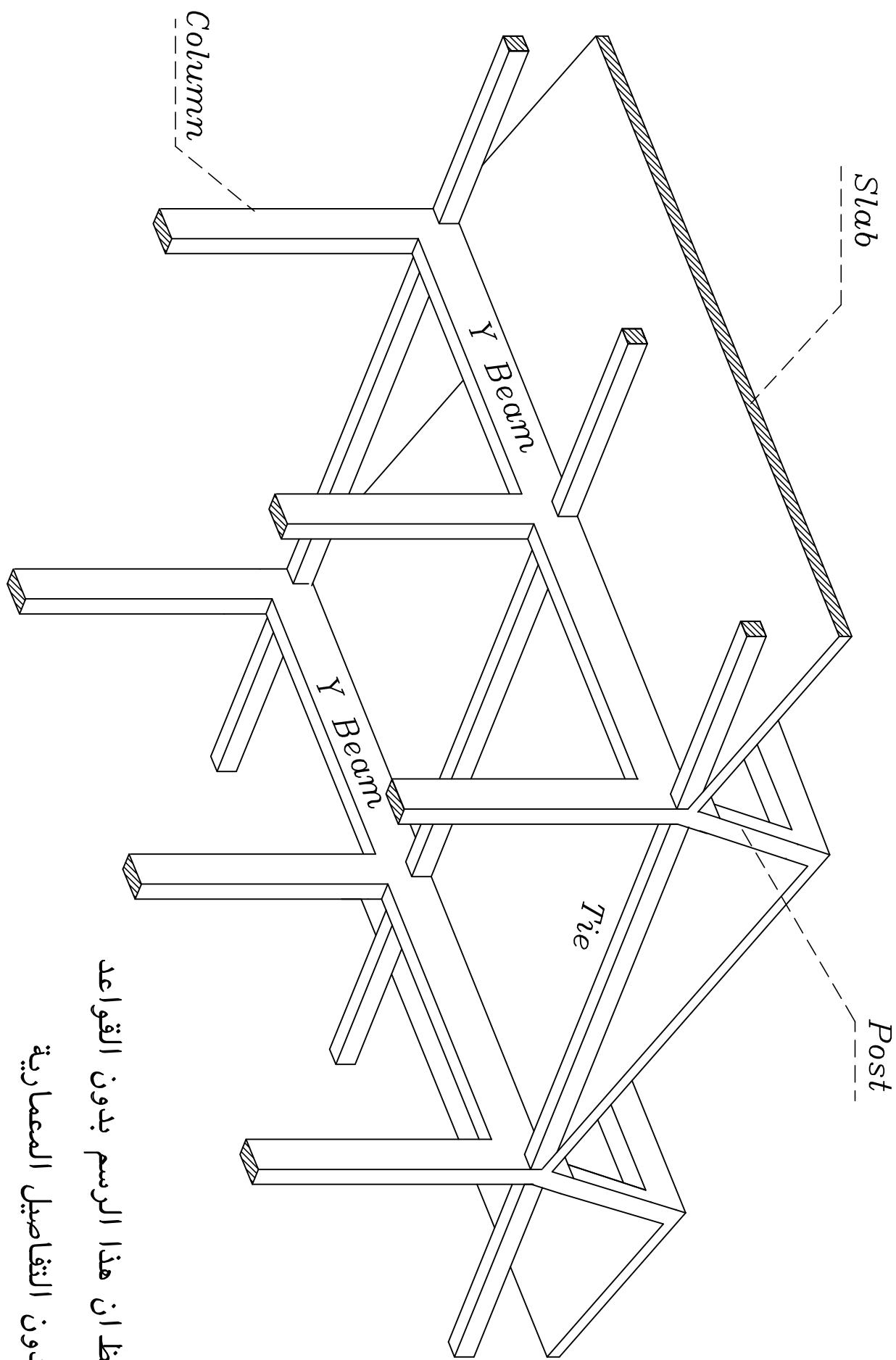
٢ - تقليل العزم الموجب للبلاطة

٣ - عدم سقوط مياه المطر مباشرة على الشباك

# حاول ان تتخيل عناصر ال System



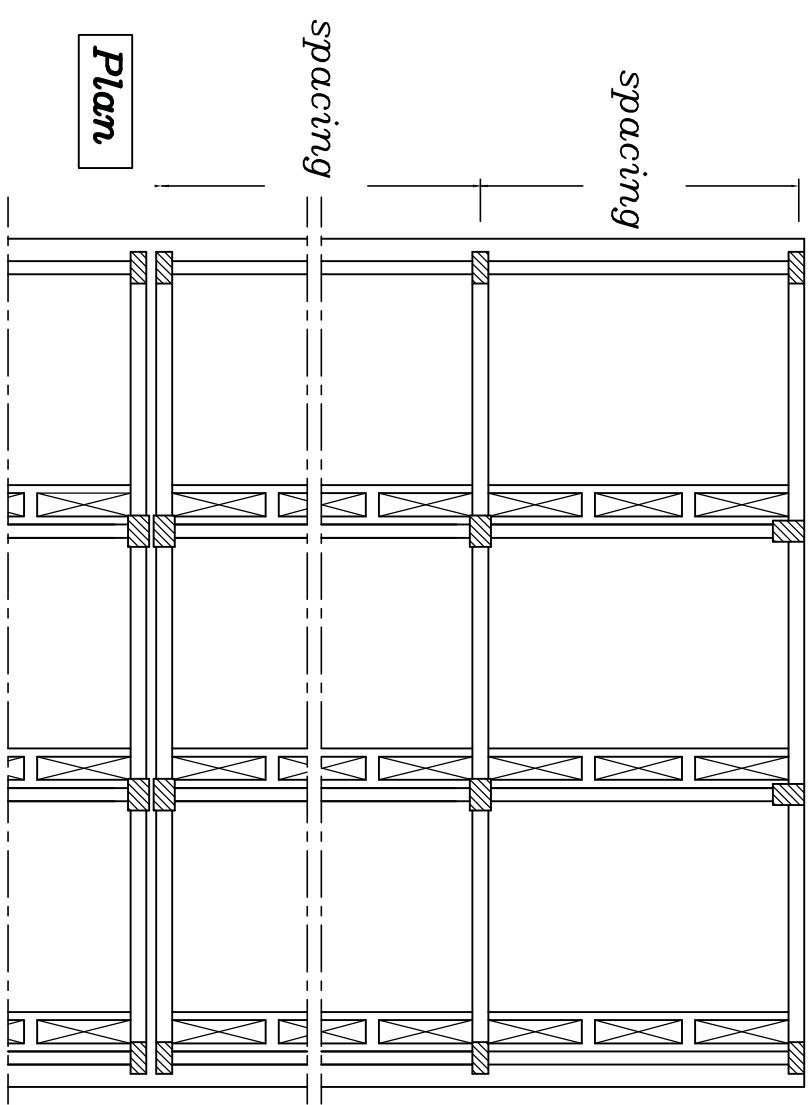
لا حظ ان هذا الرسم بدون السلاط  
و بدون التفاصيل المعمارية



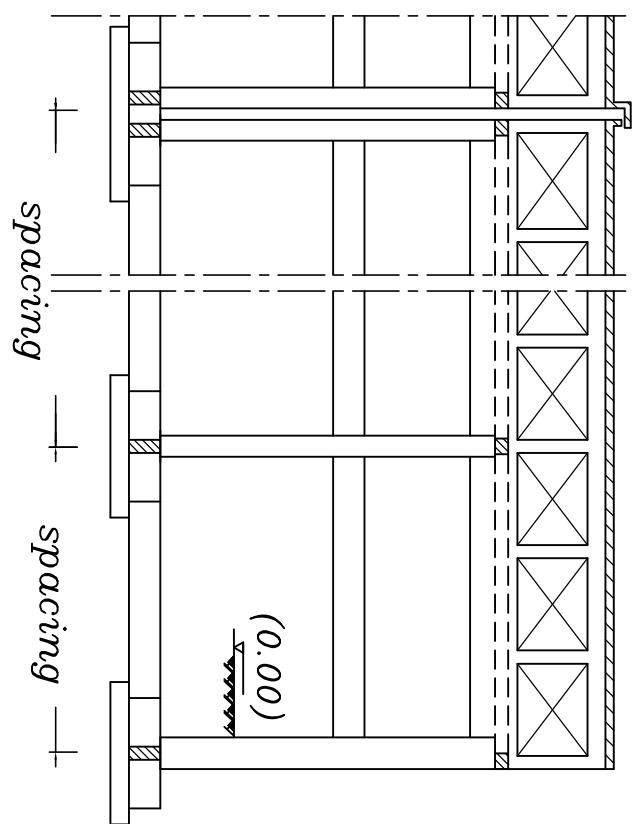
لاحظ أن هذا الرسم بدون القواعد  
وبدون التفاصيل المعمارية

1:200 → 1:400

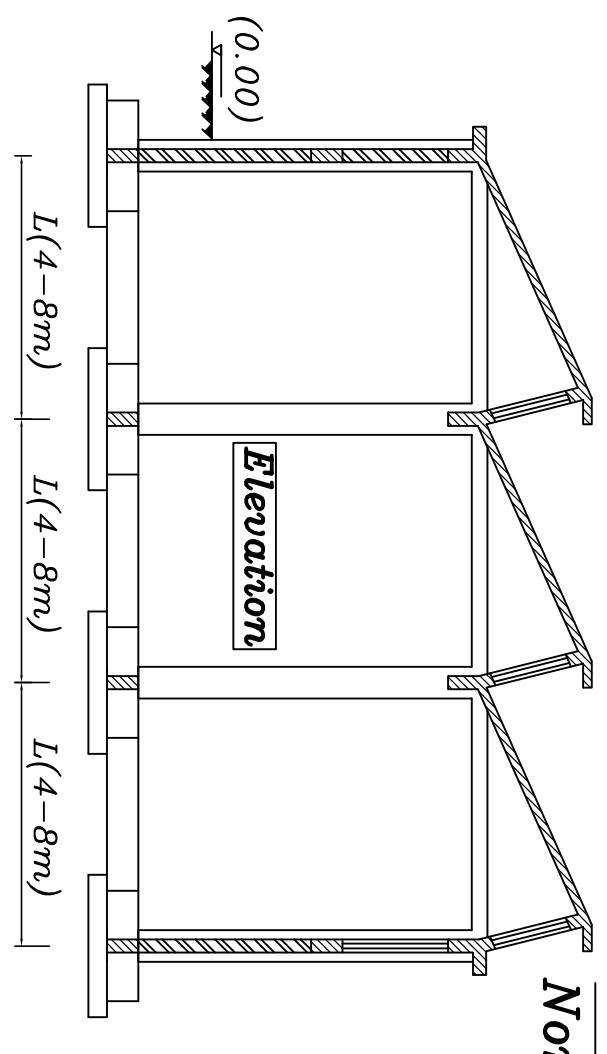
**KEY PLAN**



**Plan**



**Side view**



**Elevation**

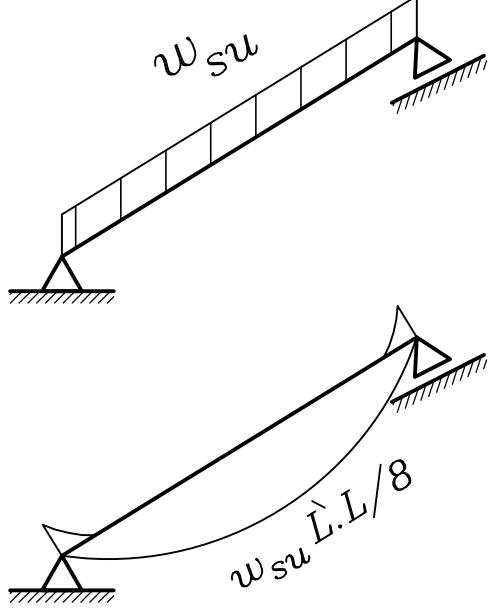
North

# Steps of design

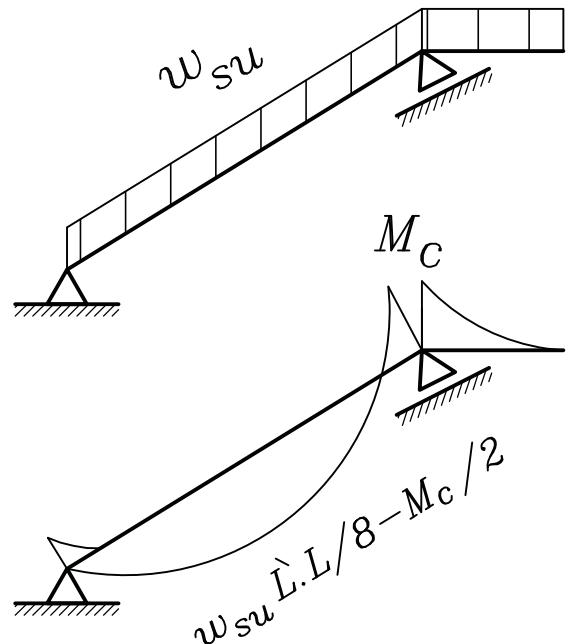
## 1] Analysis of Slabs

$$w_{su} = 1.4 [t_s \gamma_c + F.c.] + 1.6 L.L. \cos \theta \quad (\text{for S.S.})$$

$$w_{su} = 1.4 [t_s \gamma_c + F.c. + 2bh\gamma_c + 10 * \text{w.t. of Block}] + 1.6 L.L. \cos \theta \quad (\text{for H.B.})$$

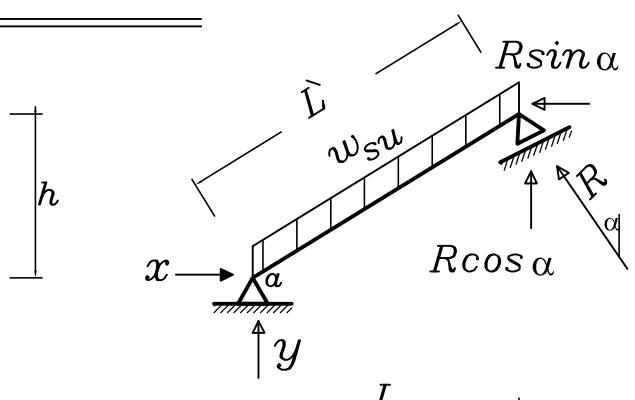


no cantilever



Case of cantilever

## 2] Reactions of slabs on beams



$$\sum M_a = 0$$

$$w_{su} L \cdot \frac{L}{2} = R(\cos \alpha) * L + R(\sin \alpha) * h \implies \text{get } R$$

$$\sum y = 0 \quad w_{su} L - y - R \cos \alpha = 0 \implies \text{get } y$$

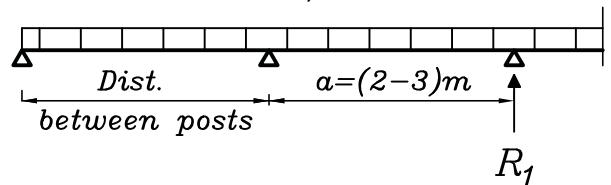
$\sum x = 0$  By Eng. R. Mostafa & Eng. Yasser M. Samir

### 3]Analysis of Ridge beam(250\*400)

$$w = R + o.w$$

$$kN/m$$

$$w \quad kN/m^{'}$$



$$R_1 = w * a$$

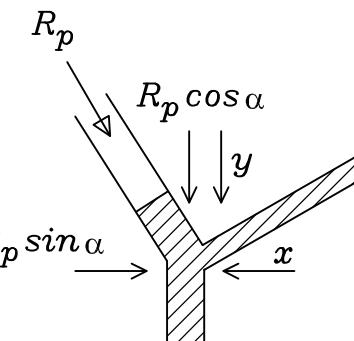
### 4]Design of Posts

$$R_p = R_1 + o.w \text{ of Post}$$

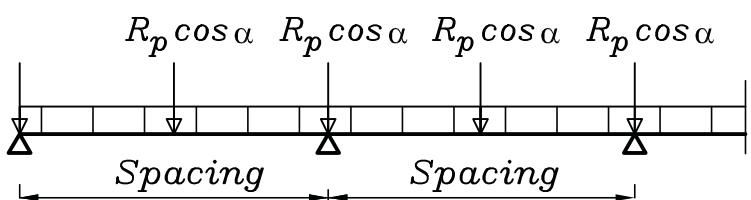
$$R_p = 0.35A_c f_{cu} + 0.67A_s f_y \quad \rightarrow \text{get } A_s$$

### 5]Design of Y-beam

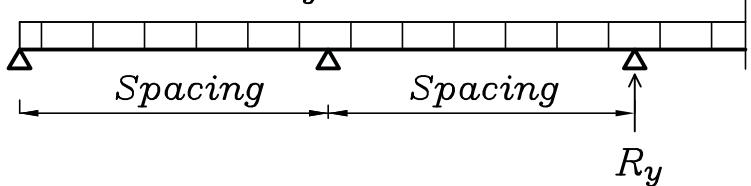
$$w_y = o.w + y + \frac{\Sigma R_p \cos \alpha}{Span} \quad kN/m$$



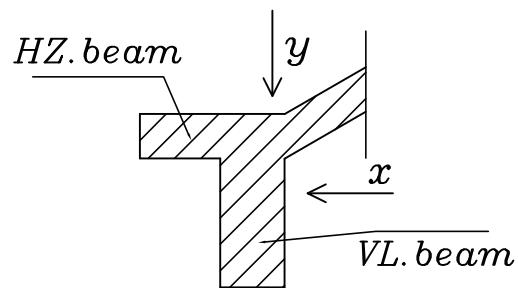
$$R_y = w_y * \text{Spacing}$$



$$w_y \quad kN/m^{'}$$



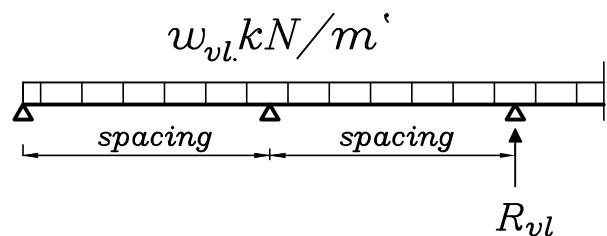
## 6]Analysis of End beam



### For VL. beam

$$w_{vl.} = o. w + y \quad kN/m$$

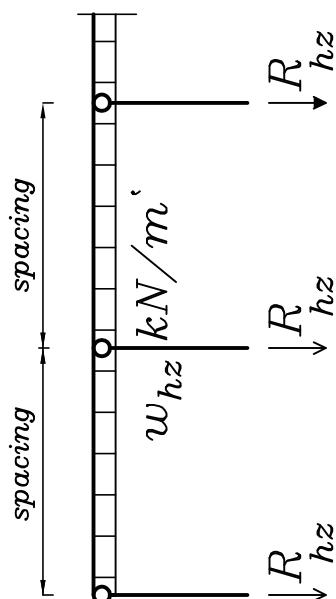
$$R_{vl} = w_{vl} * Spacing$$



### For HZ. beam

$$w_{hz} = x \quad kN/m$$

$$R_{hz} = w_{hz} * Spacing$$



## 7]Design of Tie

$$T = R_{hz} = w_{hz} * Spacing$$

$$A_s = \frac{T_u}{f_y / \gamma_s}$$

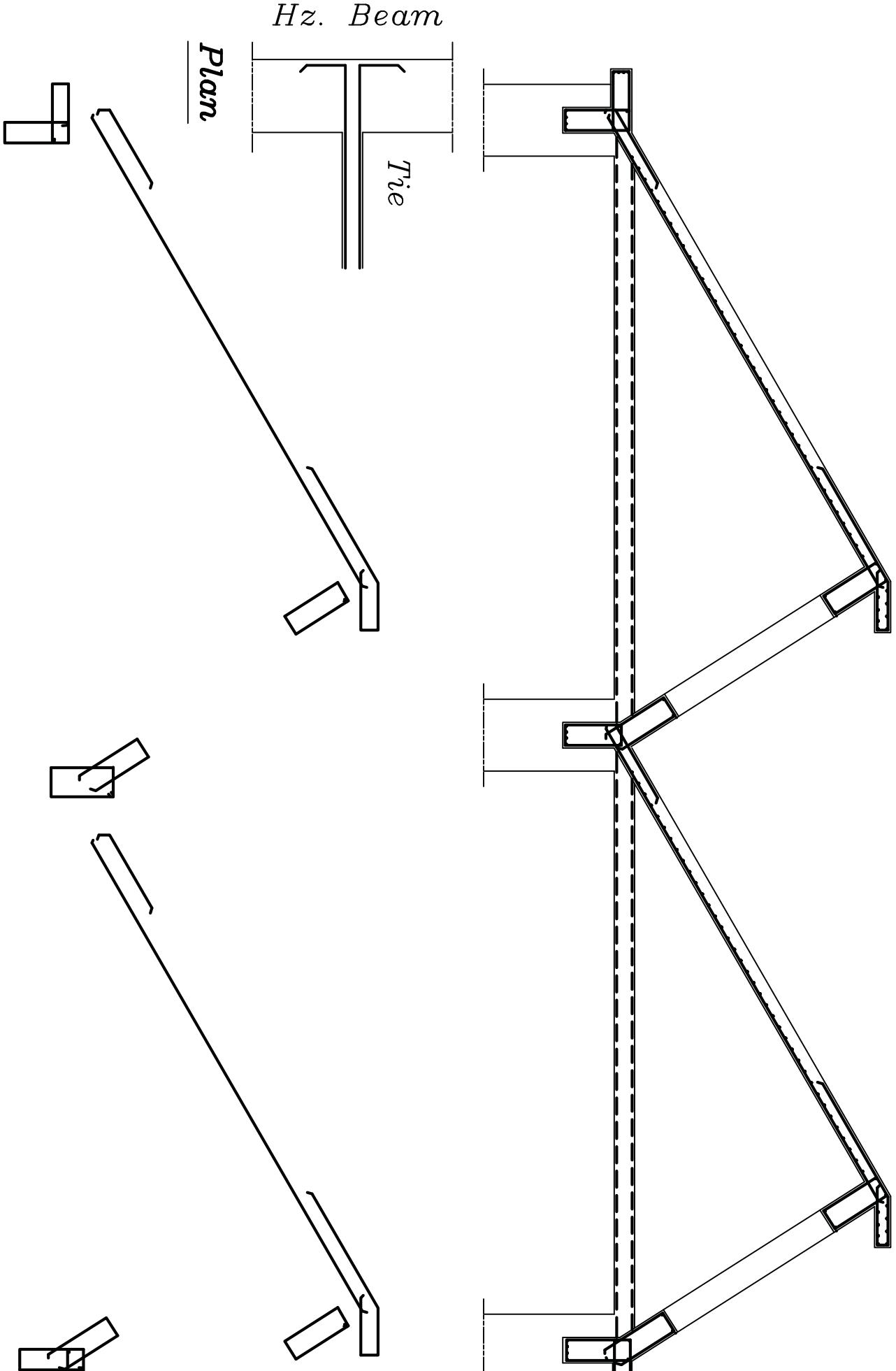
## 8]Design of Col.

$$P_{col.} = R_{y-beam}$$

Design  $N, M_{add.}$

By Eng. Ezz El-Din Mostafa & Eng. Yasser M. Samir

## Details of R.F.T.



## Example

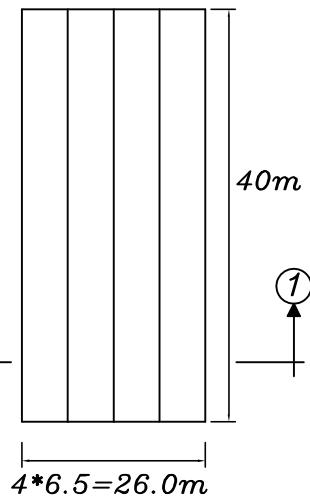
North

For the given plan and cross-section,  
it is required to:

1-Choose the suitable system to cover  
this Area.

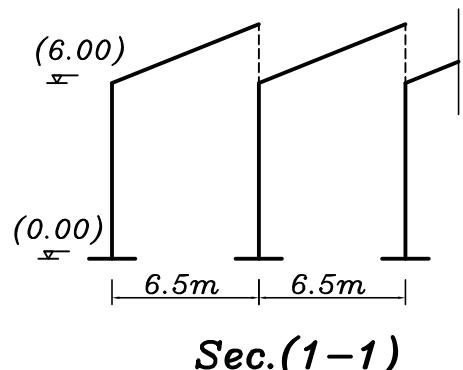
2-Design all Slabs and draw plan of Rft.

3-Design Ridge, Column, Post  
and draw details of Rft.



$$F.C. = 1.4 \text{ kN/m}^2, L.L = 0.5 \text{ kN/m}^2$$

$$f_{cu} = 25 \text{ N/mm}^2, f_y = 360 \text{ N/mm}^2$$



## Solution

$$t = \frac{716}{16} = 44.75 \text{ cm}$$

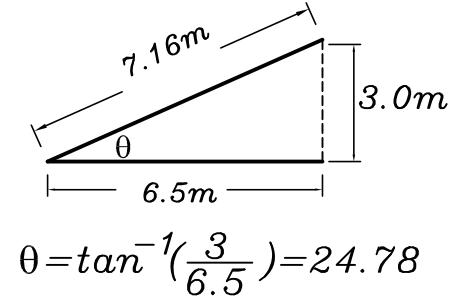
take  $t = 25 \text{ cm}$  [20cm+5cm]

$$w_{su} = \frac{1.4[t_s \delta_c * (e+b) + b h \delta_c + 5 * \text{wt. of block}]}{(e+b)}$$

$$w_{su} = \frac{1.4[0.05*25*0.5 + 0.1*0.2*25 + 5*0.16]}{0.50} + 1.4*1.4 + 1.6*0.5*0.91$$

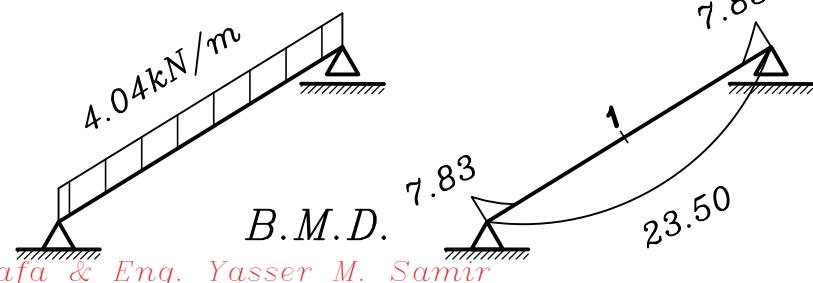
$$= 8.08 \text{ kN/m}^2$$

$$w_{su/Rib} = 0.5*8.2 = 4.04 \text{ kN/m}^2$$



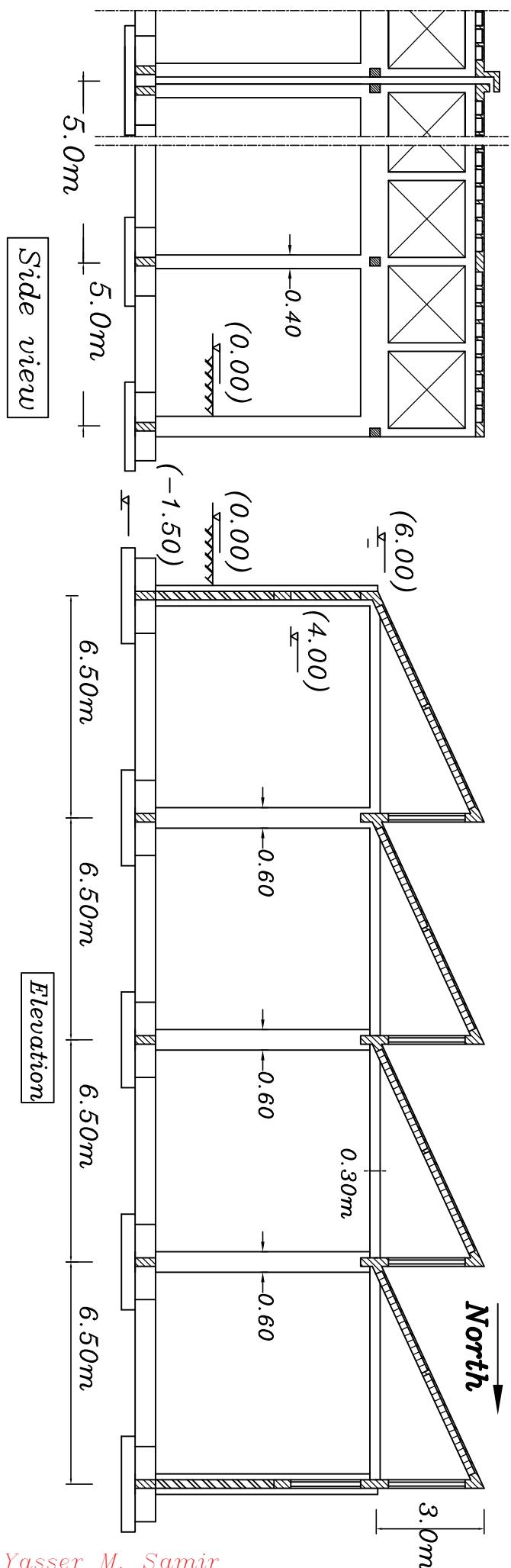
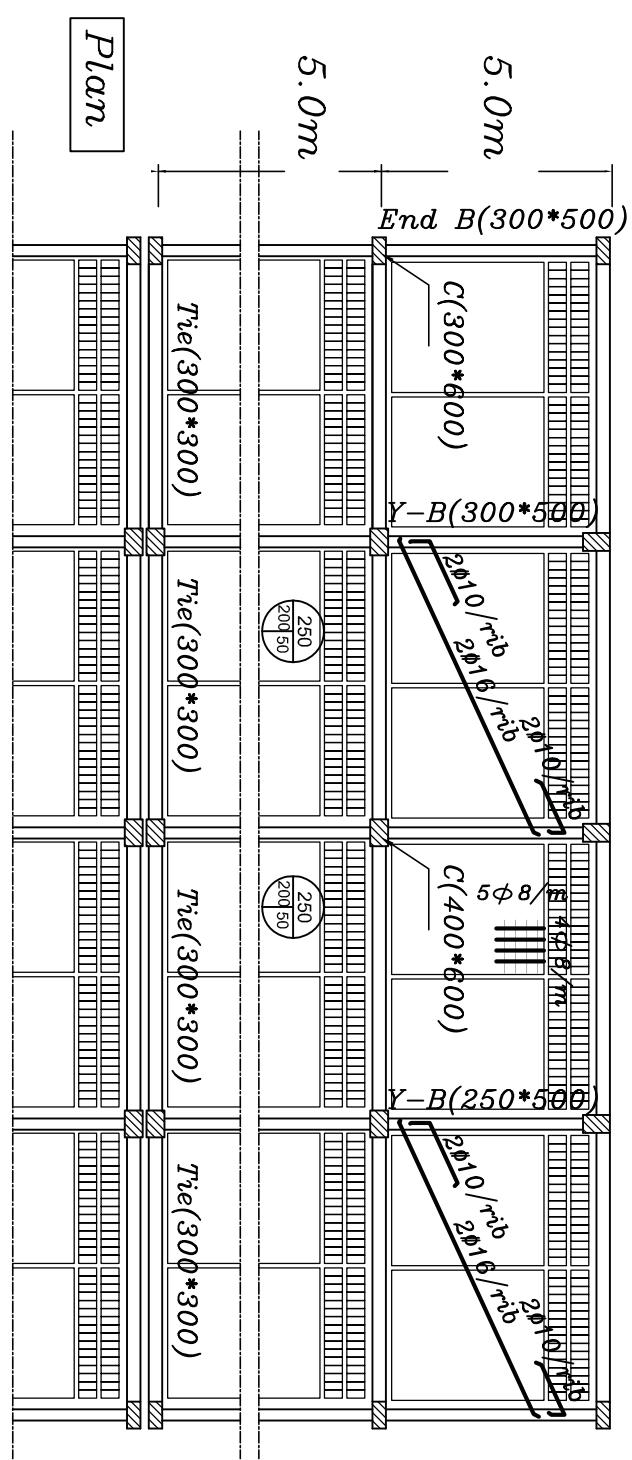
$$\theta = \tan^{-1}(\frac{3}{6.5}) = 24.78$$

$$+ 1.4F.C. + 1.6L.L. \cos\theta$$



KEY PLAN

1:200 → 1:400



## Sec. (1-1)

$$220 = C_1 \sqrt{\frac{23.50 \times 10^6}{500 \times 25}} \quad C_1 = 5.07 \quad J = 0.826$$

$$A_s = \frac{23.50 \times 10^6}{0.826 \times 360 \times 220} = 3.59 \text{ cm}^2/\text{rib}$$

$$A_s = 2 \phi 16/\text{rib}$$

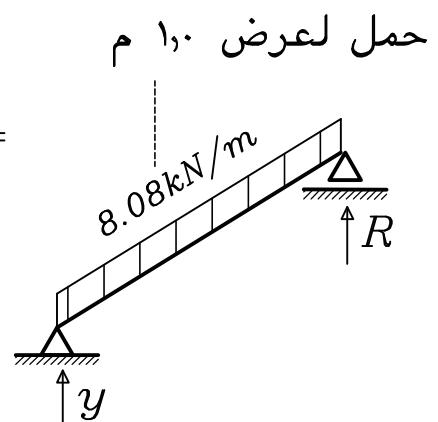
## Sec. (2-2)

$$A_s = 2 \phi 10/\text{rib}$$

## 2] Reactions of slabs on beams

$$R = y = w_{su} \frac{L}{2} \quad \text{kN/m}$$

$$R = y = 8.08 \times 7.16 / 2 = 28.93 \text{ kN/m}$$



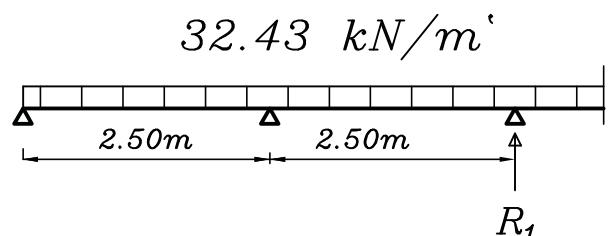
## 3] Design of Ridge beam (250\*400)

$$w = R + o.w \quad \text{kN/m}$$

$$w = 28.93 + 0.25 \times 0.40 \times 25 \times 1.40$$

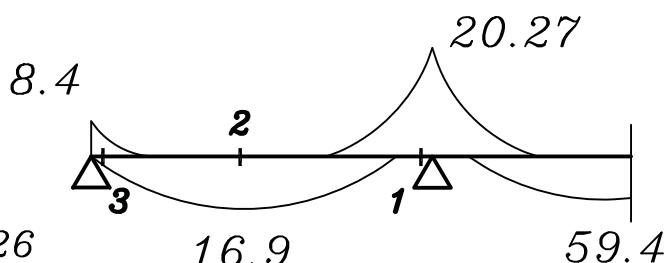
$$w = 32.43 \text{ kN/m}$$

$$R_1 = 32.43 \times 2.5 = 81.08 \text{ kN}$$



$$\text{Sec 1} \quad M_{u.l.} = 20.27 \text{ kN.m}$$

$$350 = C_1 \sqrt{\frac{20.27 \times 10^6}{25 \times 250}} \rightarrow C_1 = 6.1 \rightarrow J = 0.826$$

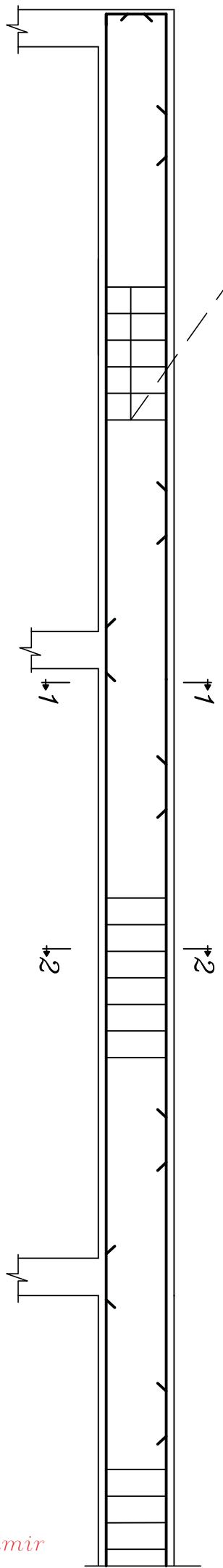


$$A_s = \frac{20.27 \times 10^6}{360 \times 0.826 \times 350} = 194.7 \text{ mm}^2$$

Use  $\min A_s = 2 \phi 12$   
By Eng. Ezz El-Din Mostafa & Eng. Yasser M. Samir

## *Detail of reinforcement of Ridge beam*

508/m



2012 — 2010

2012

2012  
2010  
set

2012

6106

2012

Technical drawing of a rectangular component with four corner holes and a central slot, labeled 2012. The component is shown in two orientations, one above the other. The top orientation shows the component with a central slot and four corner holes. The bottom orientation shows the component with a central slot and four corner holes, with the text '2010' written at the bottom right corner.

40.25

Sec. (1-1)

† 0.25

Sec. (2-2)

## 4]Design of Posts

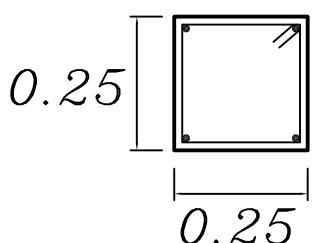
$$R_p = R_1 + o.w \text{ of Post}$$

$$R_p = 81.08 + 0.25 * 0.25 * 3 * 25 * 1.40 = 87.64 \text{ kN}$$

$$87.64 * 10^3 = 0.35 * 250 * 250 * 25 + 0.67 A_s f_y$$

$$A_s = -ve \rightarrow A_s = 4\phi 12$$

4φ12



## 5]Design of Y-beam (300\*500)

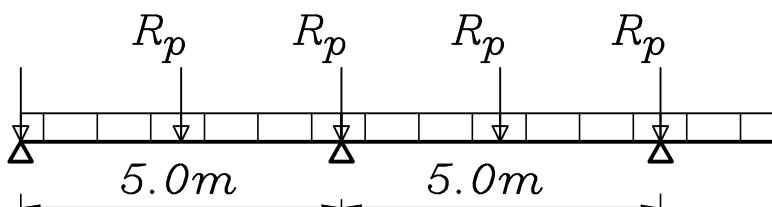
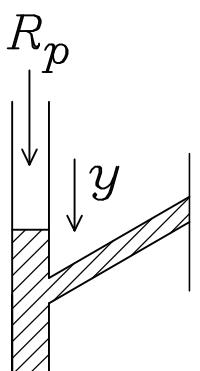
$$w_y = o.w. + y + \frac{\Sigma R_p}{Span} \text{ kN/m}$$

$$w_y = 0.30 * 0.50 * 25 * 1.40 + 28.93 + \frac{2 * 87.64}{5.0}$$

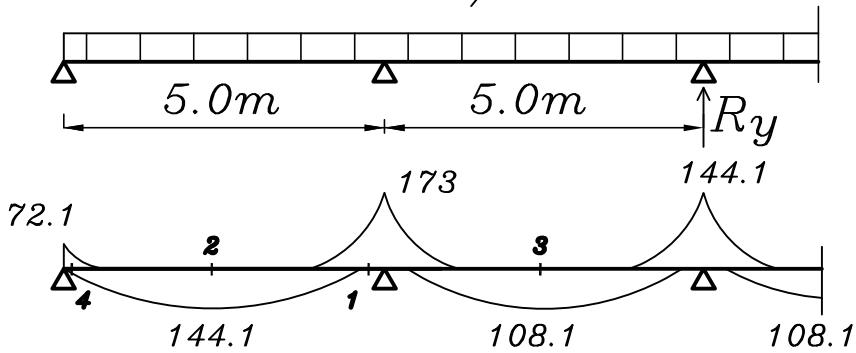
$$w_y = 69.2 \text{ kN/m}$$

$$R_y = 69.2 * 5.0 = 346 \text{ kN}$$

نصيب البحر الواحد  
هو حمل في وسطه و نصف حمل من  
كل ركبة



$$69.2 \text{ kN/m}^'$$



Sec 1  $M_{u.l.} = 173 \text{ kN.m}$

$$450 = C_1 \sqrt{\frac{173*10^6}{25*300}} \rightarrow C_1 = 2.96 \rightarrow J = 0.74$$

$$A_s = \frac{173*10^6}{360*0.74*450} = 1443 \text{ mm}^2 \quad A_s = 6 \phi 18$$

Sec 2  $M_{u.l.} = 144.1 \text{ kN.m}$

$$450 = C_1 \sqrt{\frac{144.1*10^6}{25*300}} \rightarrow C_1 = 3.24 \rightarrow J = 0.76$$

$$A_s = \frac{144.1*10^6}{360*0.76*450} = 1170 \text{ mm}^2 \quad A_s = 5 \phi 18$$

Sec 3  $M_{u.l.} = 108.1 \text{ kN.m}$

$$450 = C_1 \sqrt{\frac{108.1*10^6}{25*300}} \rightarrow C_1 = 3.75 \rightarrow J = 0.79$$

$$A_s = \frac{108.1*10^6}{360*0.79*450} = 845 \text{ mm}^2 \quad A_s = 4 \phi 18$$

Sec 4  $M_{u.l.} = 72.1 \text{ kN.m}$

$$450 = C_1 \sqrt{\frac{72.1*10^6}{25*300}} \rightarrow C_1 = 4.6 \rightarrow J = 0.82$$

$$A_s = \frac{72.1*10^6}{360*0.82*450} = 543 \text{ mm}^2 \quad A_s = 3 \phi 16$$

check  $A_{smin}$  safe

Check shear

$$Q_{su} = 207.6 \text{ kN}$$

$$q_{su} = \frac{Q_{cr}}{bd} = \frac{207.6*10}{300*450} = 1.54 \text{ N/mm}^2$$

$$q_{cu} = 0.24 \sqrt{\frac{25}{1.5}} = 0.98 \text{ N/mm}^2$$

$$q_{max} = 0.7 \sqrt{\frac{25}{1.5}} = 2.86 \text{ N/mm}^2 \quad q_{cu} < q_u < q_{umax}$$

$$q_u - \frac{q_{cu}}{2} = \frac{nA_s f_y / \gamma_s}{bS}$$

assume  $n=2$

$$A_s = 78.5 \text{ mm}^2 = \phi 10$$

$$1.54 - \frac{0.98}{2} = \frac{2*78.5*240/1.15}{300*S} \implies S = 104 \text{ mm}$$

$$\text{No. of stirrups}/m = \frac{1000}{S} = 9.7 \quad \text{Take Stirrups } 10\phi 10/m$$

## 6] Analysis of End beam

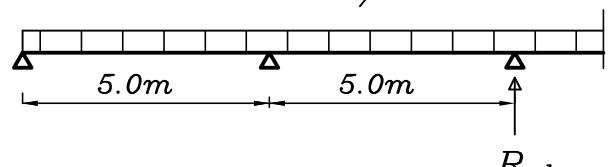
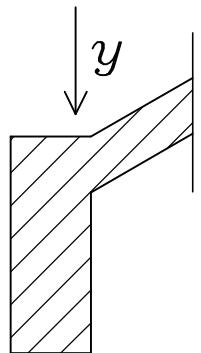
$$w_{vl} = o.w + y \quad \text{kN/m}$$

$$w_{vl} = 0.25 * 0.50 * 25 * 1.40 + 28.93$$

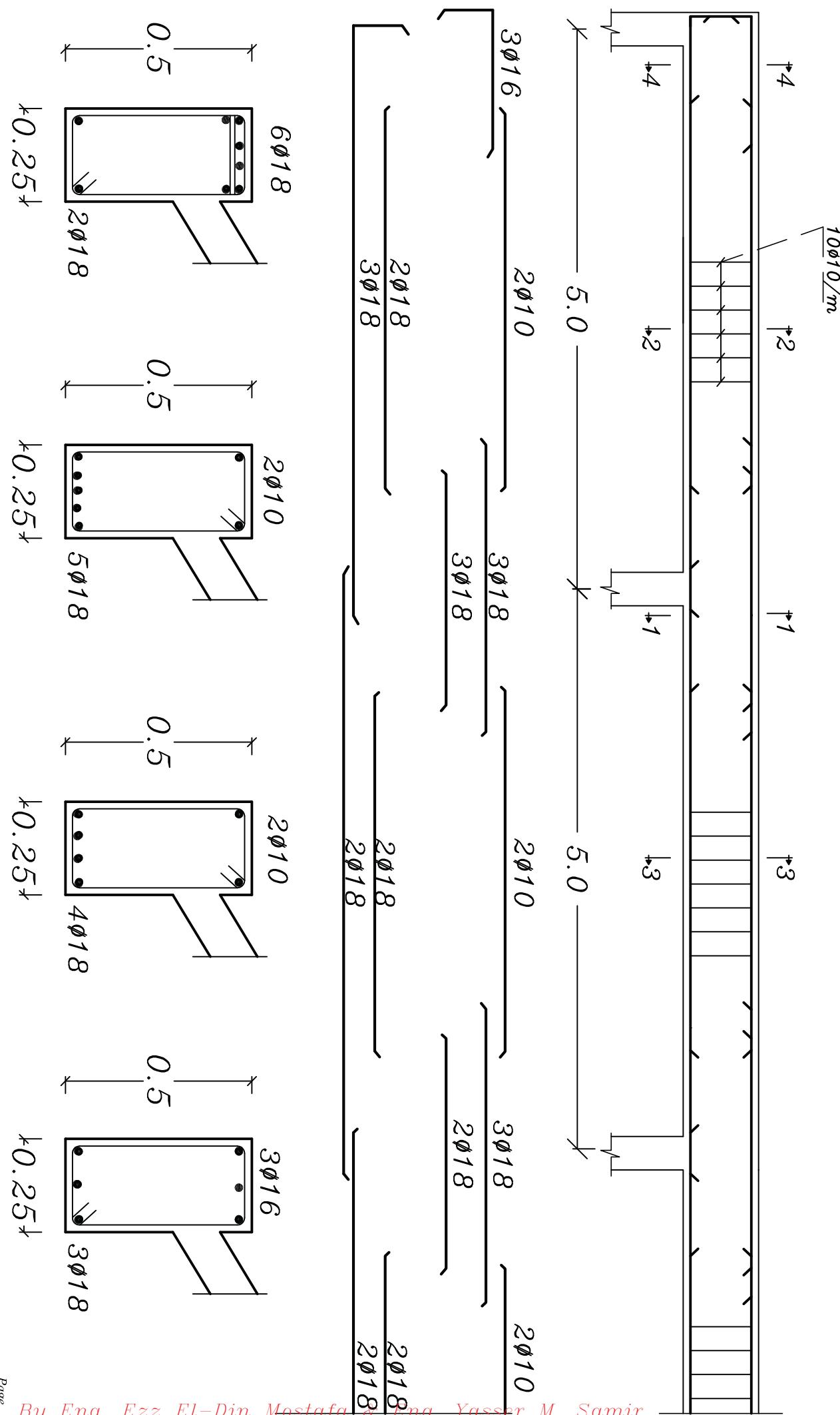
$$w_{vl} = 33.31 \text{ kN/m} \quad 33.31 \text{ kN/m}$$

$$R_{vl} = 33.31 * 5.0 = 166.53 \text{ kN}$$

ثم تصميم مثل الـ *Y-beam*



# Detail of reinforcement of Y-beam



Sec.(1-1)

Sec.(2-2)

Sec.(3-3)

Sec.(4-4)

## 8]Design of Col. (400\*600)

$$P_{col.} = 341.81 \text{ kN}$$

$$\lambda_{b_{in}} = \frac{1.3*6.75}{0.60} = 14.63$$

$$\lambda_{b_{out}} = \frac{1.2*6.25}{0.40} = 18.75$$

Buckling outside plan

$$\delta_b = \frac{\lambda_b^2 b}{2000} = \frac{18.75^2 * 0.40}{2000} = 0.07 \text{ m}$$

$$M_{add} = 341.81 * 0.07 = 24.03 \text{ kN.m}$$

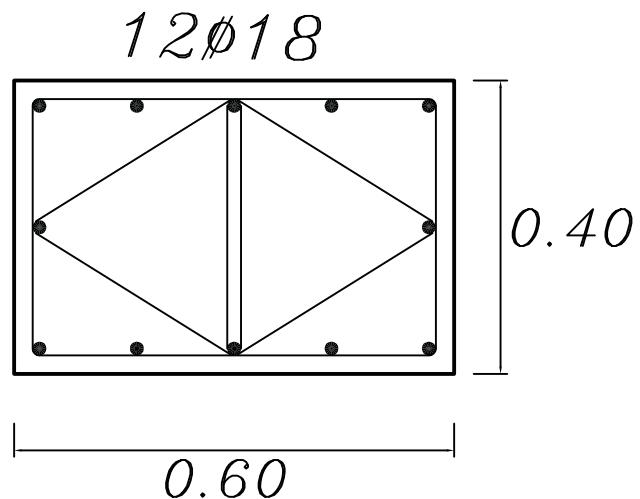
$$\frac{N_{u.l.}}{bt f_{cu}} = \frac{341.81 * 10^3}{400 * 600 * 25} = 0.06 \quad \zeta = \frac{400 - 100}{400} = 0.75$$

$$\frac{M_{u.l.}}{bt^2 f_{cu}} = \frac{24.03 * 10^6}{600 * 400^2 * 25} = 0.01$$

$\rho < 1$  Take  $\rho = 1$

$$A_{s \ min} = \frac{0.25 + 0.052 * 18.75}{100} * 400 * 600 = 2940 \text{ mm}^2$$

$$A_s = 12 \phi 18$$



## Example

For the given plan and cross-section,  
it is required to:

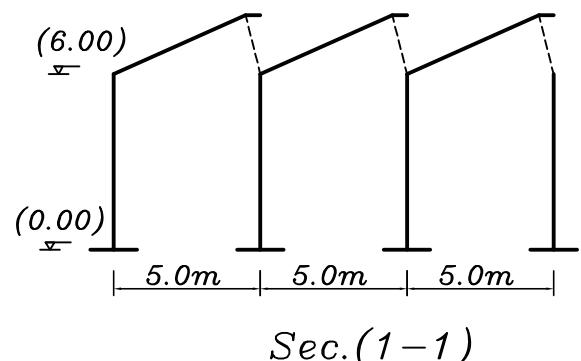
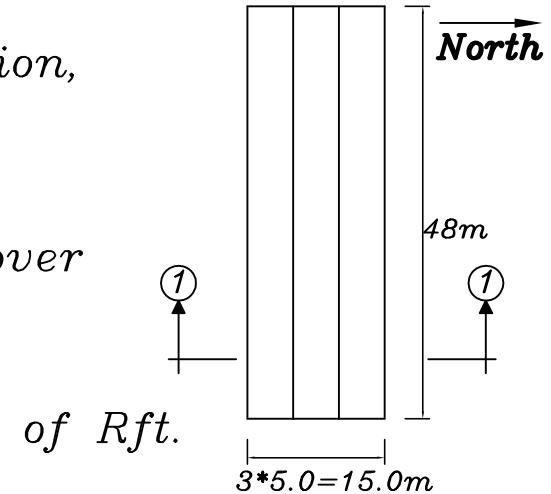
1-Choose the suitable system to cover  
this Area.

2-Design all Slabs and draw plan of Rft.

3-Design the Post, Column, Tie  
and draw details of Rft.

$$F.C. = 1.5 \text{ kN/m}^2, L.L = 0.5 \text{ kN/m}^2$$

$$f_{cu} = 25 \text{ N/mm}^2, f_y = 360 \text{ N/mm}^2$$



## Solution

$$t_s = \frac{492}{24} = 20.5 \text{ cm}$$

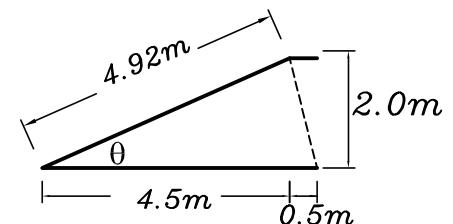
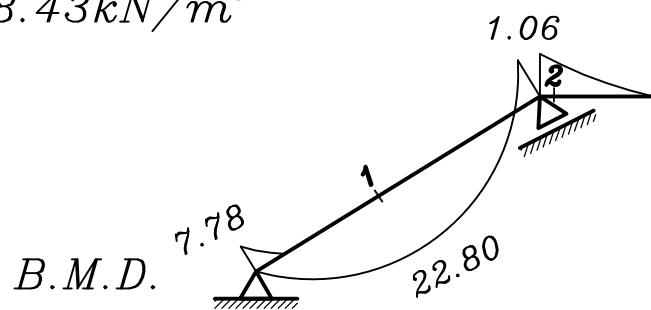
$$t_{s_{min}} = \frac{492}{35} = 14.06 \text{ cm}$$

take  $t_s = 16 \text{ cm}$  (Check def.)

$$w_{su} = 1.4[t_s \gamma_c + F.c.] + 1.6 \text{ L.L. Cos}\theta$$

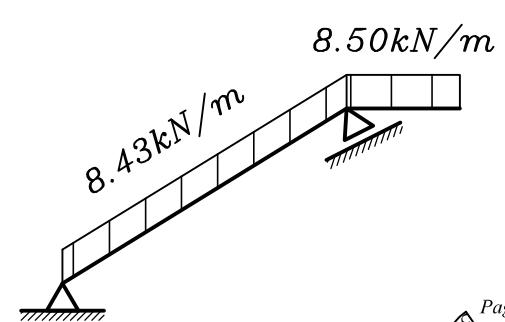
$$w_{su} = 1.4[0.16*25 + 1.5] + 1.6*0.5*0.91$$

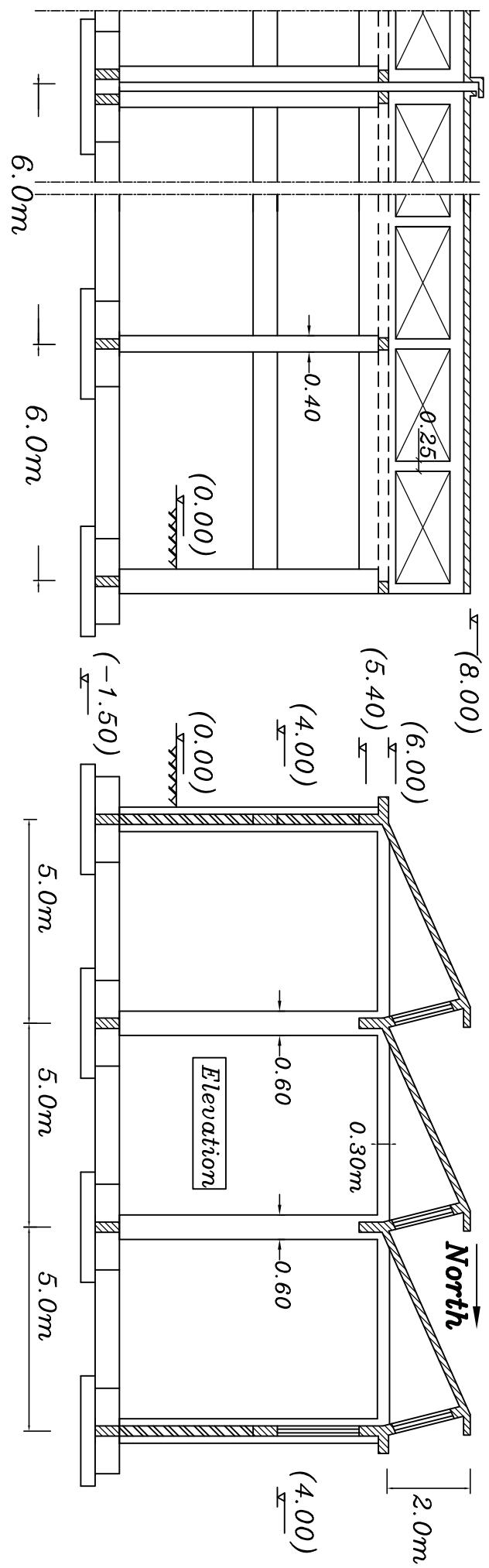
$$w_{su} = 8.43 \text{ kN/m}^2$$



$$\theta = \tan^{-1} \left( \frac{2}{4.5} \right) = 23.96$$

$$\alpha = \tan^{-1} \left( \frac{0.5}{2.0} \right) = 14.04$$





Side view

6.0m

End B(250\*600)

160

RidgeB(250\*400)

160

Y-B(250\*600)

C(300\*600)

C(400\*600)

RidgeB(250\*400)

160

Y-B(250\*600)

RidgeB(250\*400)

6.0m

Tie(300\*300)

Tie(300\*300)

Tie(300\*300)

KEY PLAN

1:200—1:400

## Sec. (1-1)

$$140 = C_1 \sqrt{\frac{22.80 * 10^6}{1000 * 25}} \quad C_1 = 4.64 \quad J = 0.821$$

$$A_s = \frac{22.80 * 10^6}{0.821 * 360 * 140} = 5.51 \text{ cm}^2/\text{m}$$

$$A_s = 5 \phi 12/\text{m}$$

## Sec. (2-2)

$$A_s = 5 \phi 8/\text{m}$$

## 2] Reactions of slabs on beams

$$\sum M_a = 0$$

$$8.43 * 4.92 * 4.5 / 2 + 8.50 * 0.5 * 4.75 = R \cos \alpha * 4.5 + R \sin \alpha * 2.0$$

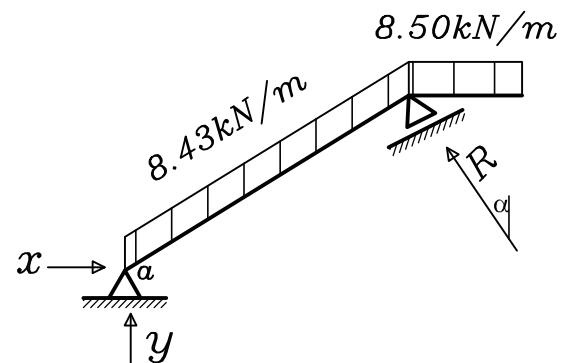
$$R = 23.40 \text{ kN/m}$$

$$\sum y = 0$$

$$8.43 * 4.92 + 8.50 * 0.5 = R \cos \alpha + y$$

$$y = 23.02 \text{ kN/m}$$

$$\sum x = 0 \quad x = R \sin \alpha = 5.68 \text{ kN/m}$$



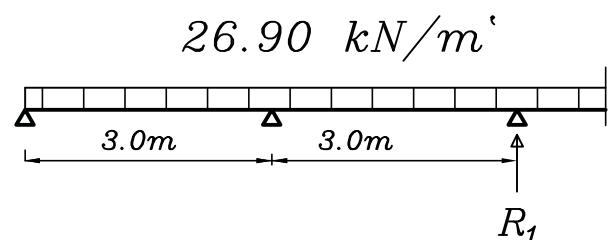
## 3] Analysis of Ridge beam (250\*400)

$$w = R + o.w \quad \text{kN/m}$$

$$w = 23.40 + 0.25 * 0.40 * 25 * 1.40$$

$$w = 26.90 \text{ kN/m}$$

$$R_1 = 26.90 * 3.0 = 80.70 \text{ kN}$$



ثم تصمم كما سبق في المسالة الاولى

## 4]Design of Posts

$$R_p = R_1 + o.w \text{ of Post}$$

$$R_p = 80.70 + 0.25 * 0.25 * 2 * 25 * 1.40 = 85.08 kN$$

$$85.08 * 10^3 = 0.35 * 250 * 250 * 25 + 0.67 A_s f_y$$

$$A_s = -ve \implies A_s = 4\#12$$

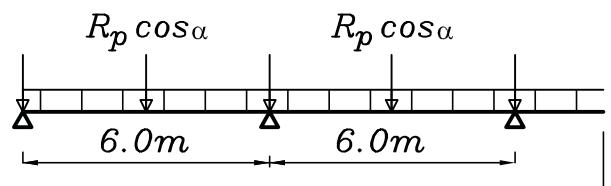
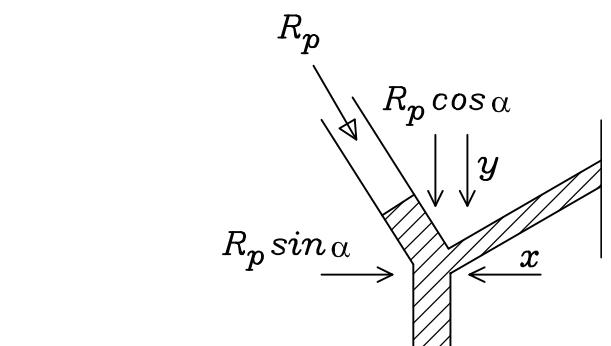
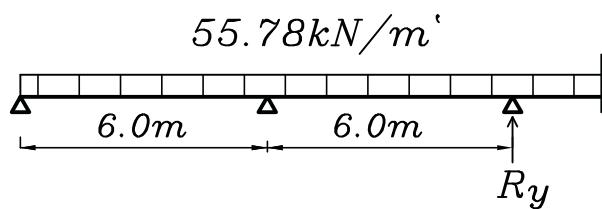
## 5]Design of Y-beam

$$w_y = o.w + y + \frac{\sum R_p \cos \alpha}{Span} \text{ kN/m}$$

$$w_y = 0.25 * 0.60 * 25 * 1.40 + 23.02 + \frac{2 * 85.08 \cos \alpha}{6.0}$$

$$w_y = 55.78 \text{ kN/m}$$

$$R_y = 55.78 * 6.0 = 334.68 \text{ kN}$$



ثم تصميم كما سبق في المسالة الاولى

## 6]Analysis of End beam

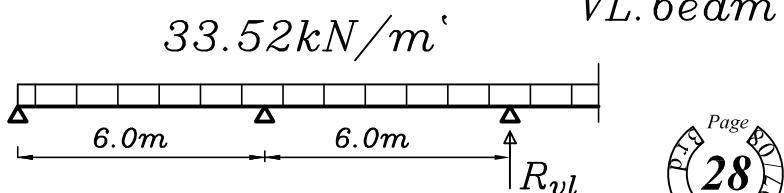
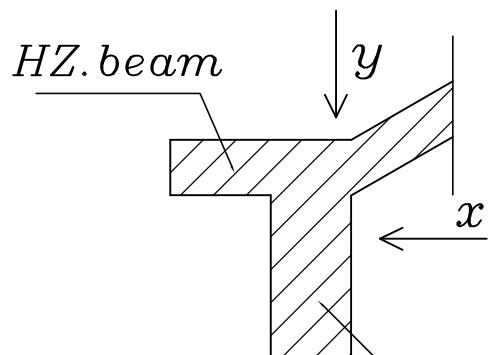
### For VL. beam

$$w_{vl} = o.w + y \text{ kN/m}$$

$$w_{vl} = 0.25 * 0.60 * 25 * 1.40 * 2 + 23.02$$

$$w_{vl} = 33.52 \text{ kN/m}$$

$$R_{vl} = 33.52 * 6.0 = 201.12 \text{ kN}$$



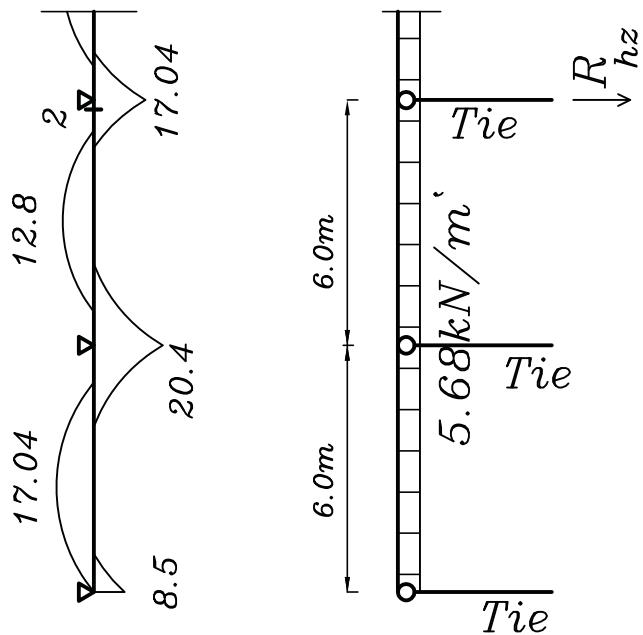
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## For HZ. beam

$$w_{hz} = x = 5.68 \text{ kN/m}$$

$$R_{hz} = 5.68 * 6.0 = 34.08 \text{ kN}$$

min. RFT



## 7]Design of Tie

$$T = R_{hz} = 34.08 \text{ kN}$$

$$A_s = \frac{34.08 * 10}{360 / 1.15^3} = 109 \text{ mm}^2$$

$$A_s = 4 \phi 12$$

## 8]Design of Col. (400\*600)

$$P_{col.} = 334.68 \text{ kN}$$

$$\lambda_{b_{in}} = \frac{1.3 * 6.75}{0.60} = 14.63$$

$$\lambda_{b_{out}} = \frac{1.2 * 6.15}{0.40} = 18.45$$

Buckling outside plan

$$\delta_b = \frac{\lambda_b^2 b}{2000} = \frac{18.45^2 * 0.40}{2000} = 0.07 \text{ m}$$

$$M_{add} = 334.68 * 0.07 = 22.79 \text{ kN.m}$$

$$\frac{N_{u.l.}}{bt f_{cu}} = \frac{334.68 * 10^3}{400 * 600 * 25} = 0.06$$

$$\zeta = \frac{400 - 100}{400} = 0.75$$

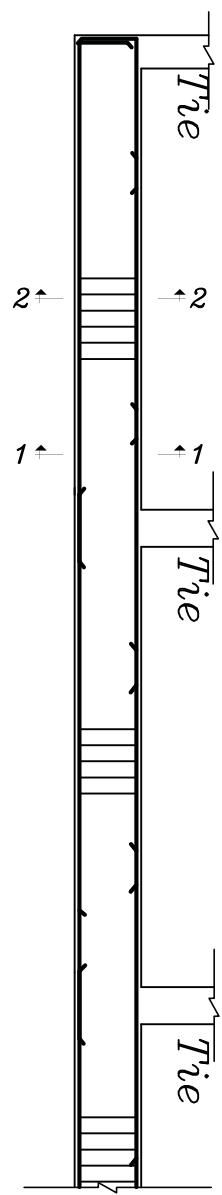
$$\frac{M_{u.l.}}{bt^2 f_{cu}} = \frac{22.79 * 10^6}{600 * 400^2 * 25} = 0.009$$

$\rho < 1$  Take  $\rho = 1$

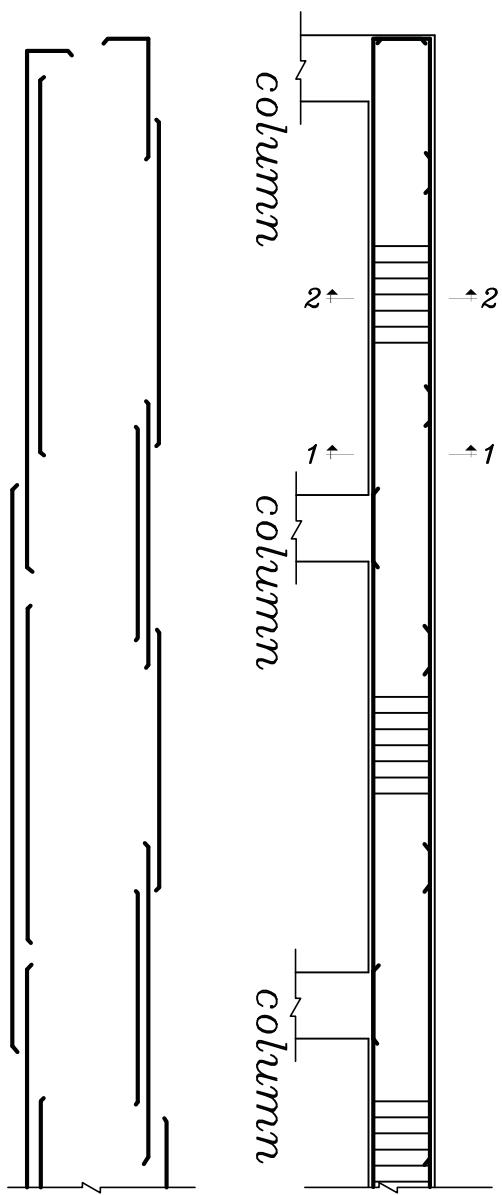
$$A_{smin} = \frac{0.25 + 0.052 * 18.45}{100} * 400 * 600 = 2903 \text{ mm}^2$$

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# R.F.T. of the VL & HZ beams

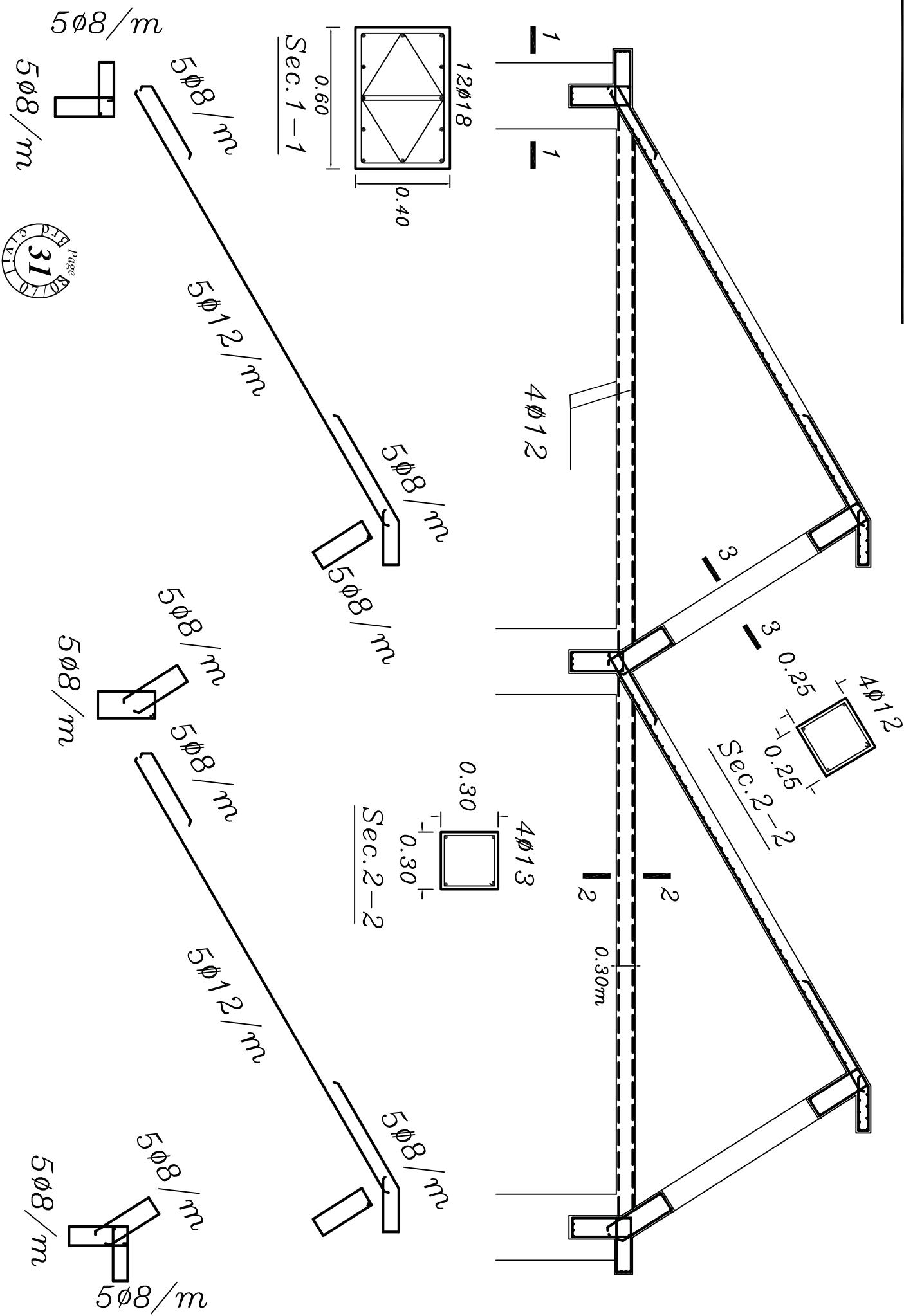


## Plan of Rft. for HL. Beam

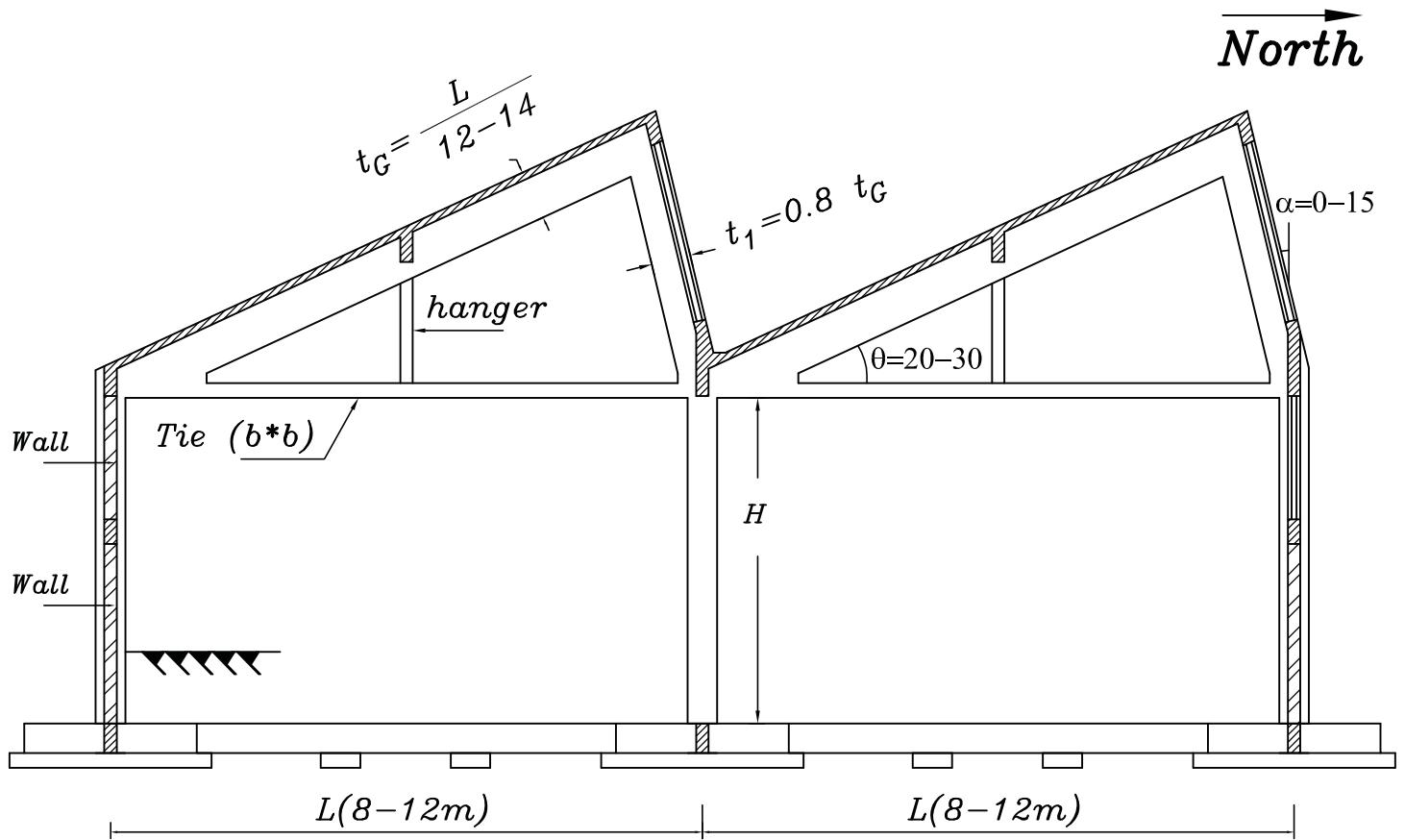


## Elev. of Rft. for VL. Beam

# Details of R.F.T.



## 2] Saw Tooth Girder Type



Saw Tooth Girder Type is used for Span (8-12m)

### Concrete Dimensions

$$t_G = \frac{L}{12-14}$$

$$t_1 = 0.8 t_G$$

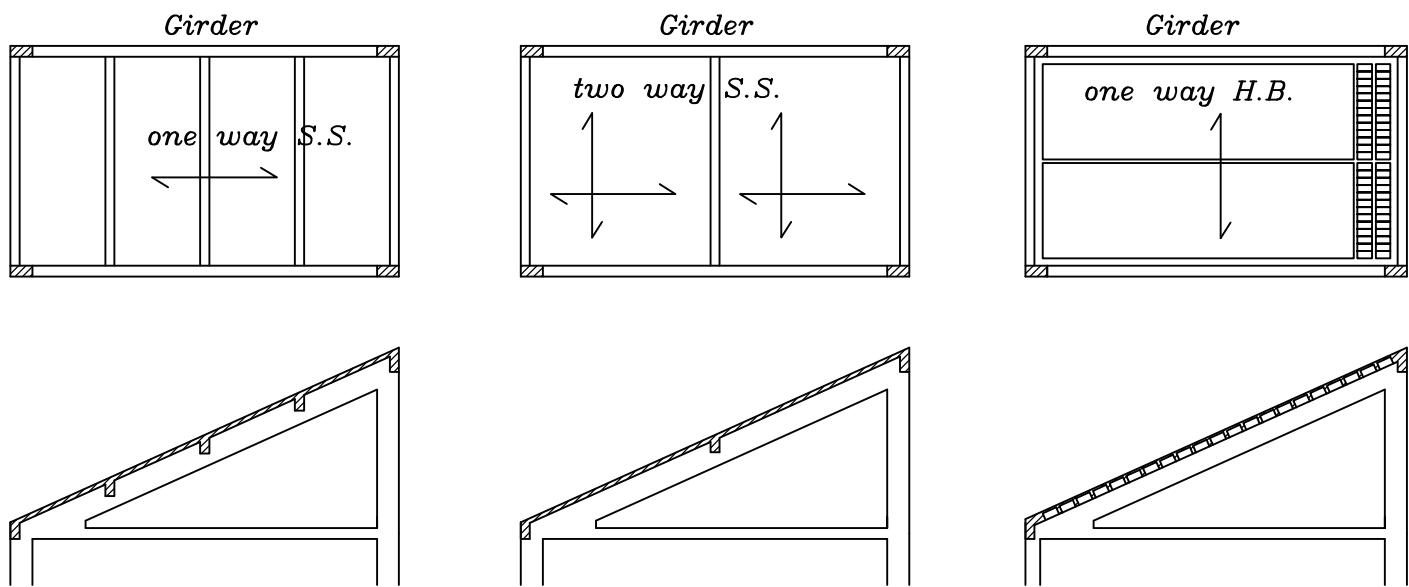
$$b = \begin{bmatrix} 30\text{cm} \\ \frac{\text{Spacing}}{20} \end{bmatrix} \quad \text{أكبر بـ}$$

Tie (b\*b) & hanger (250\*250)

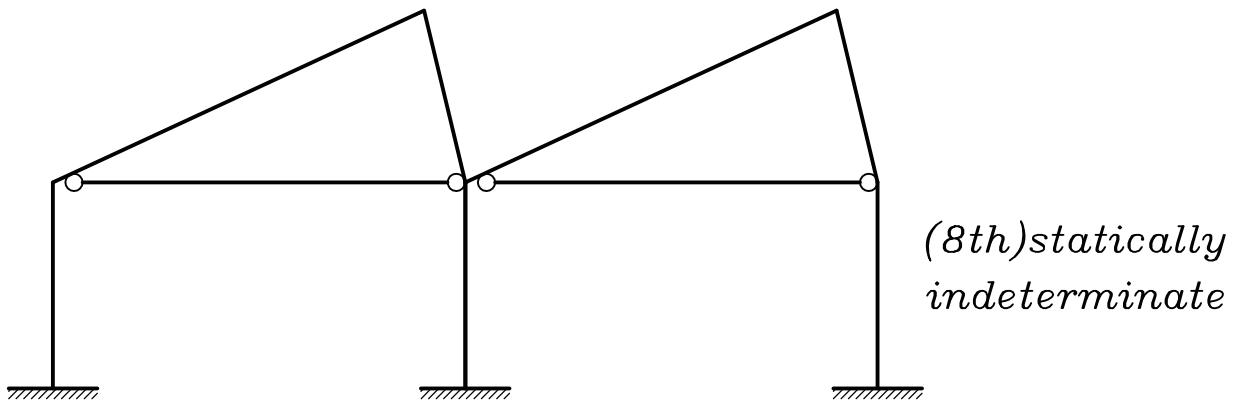
$$t(\text{col}) = \frac{H}{12}$$

# 1] Analysis of Slabs

Slabs may be H.B. Slab or Solid Slab.

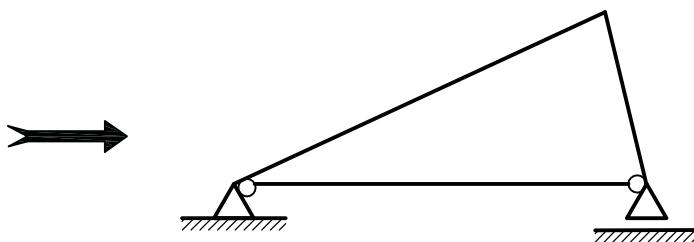


# 2] Analysis of girder

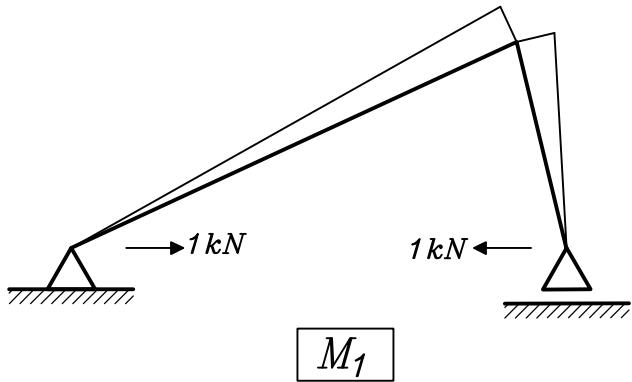


المفروض ان نحل المنشا بالكامل ولكن نظرا لصعوبة الحل سوف نهمل اتصال

الاعمدة بـ Girder ونهمل اتصال Girder ببعضها .



Using Virtual work Method (once statically indeterminate)



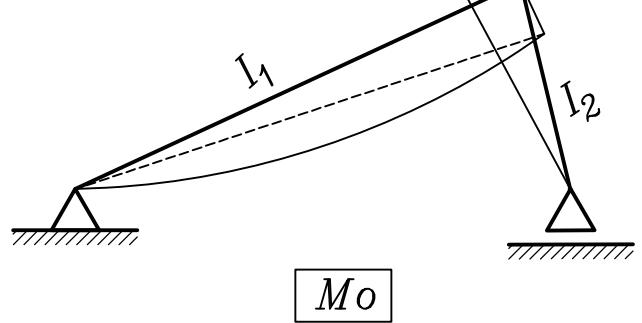
$$\delta_{10} = \frac{M_o M_1}{E_c I}$$

$$\delta_{11} = -\frac{M_1^2}{E_c I}$$

$$\delta_{10} + X \delta_{11} = 0$$

(Neglecting extension of tie)

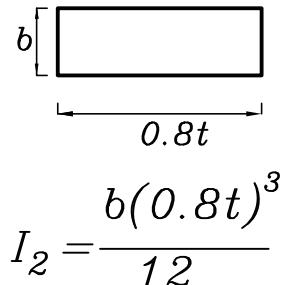
$$\delta_{10} + X \delta_{11} = 0$$



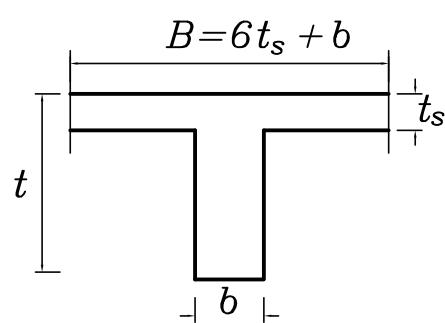
$$\delta_{10} + X \delta_{11} = 0$$

and get  $X \rightarrow$

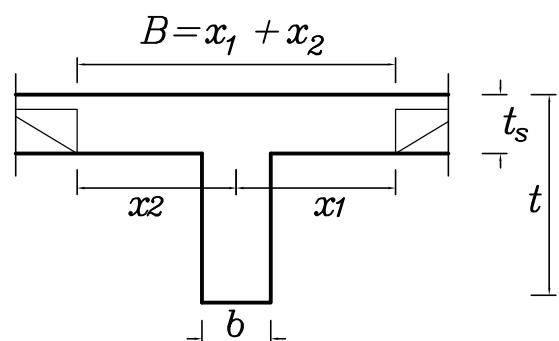
$$M_f = M_o + X M_1$$



$$I_2 = \frac{b(0.8t)^3}{12}$$



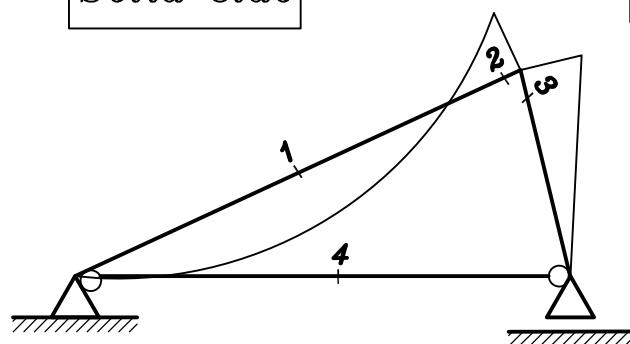
$$I_1 = \mu B t^3$$



$$I_1 = \mu B t^3$$

Solid slab

H.B. Slab



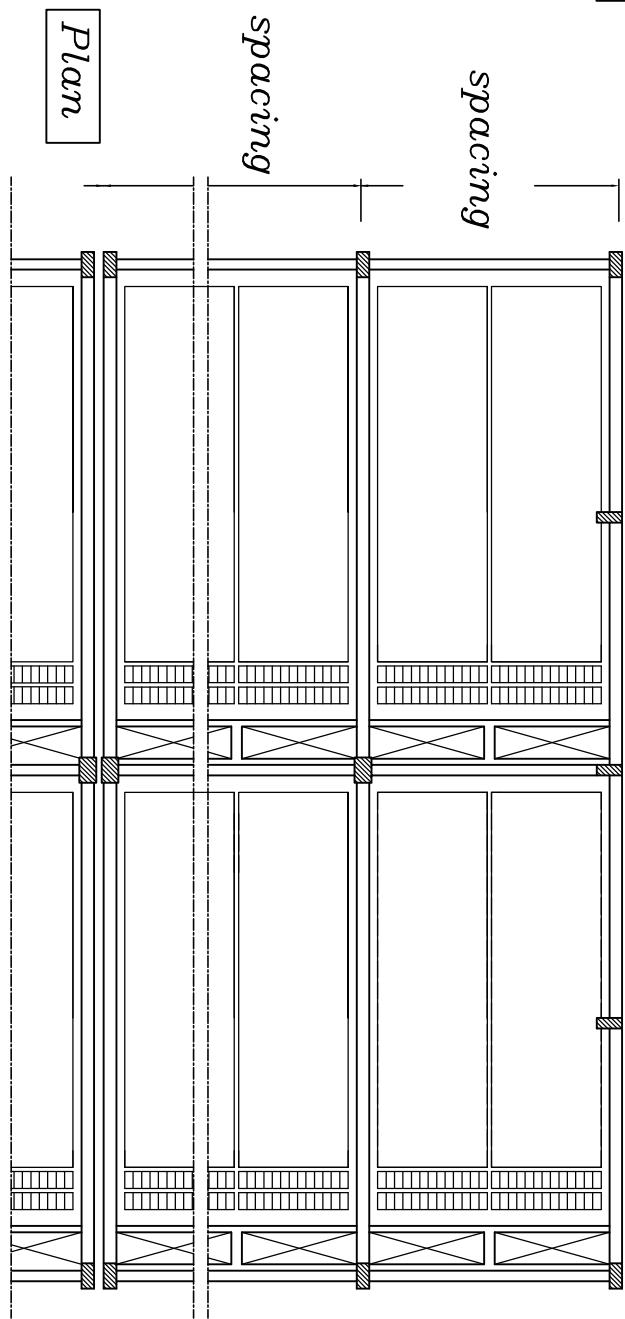
$$M_f = M_o + X M_1$$

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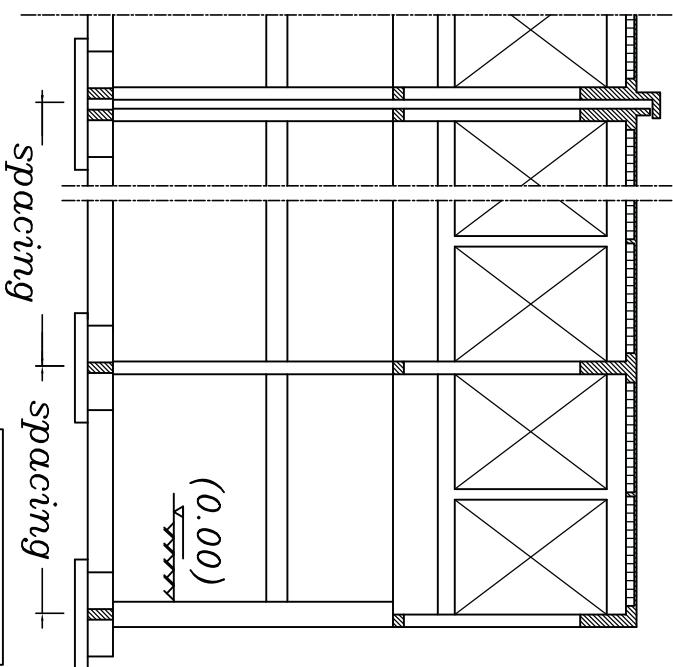
1:200—1:400

*KEY PLAN*

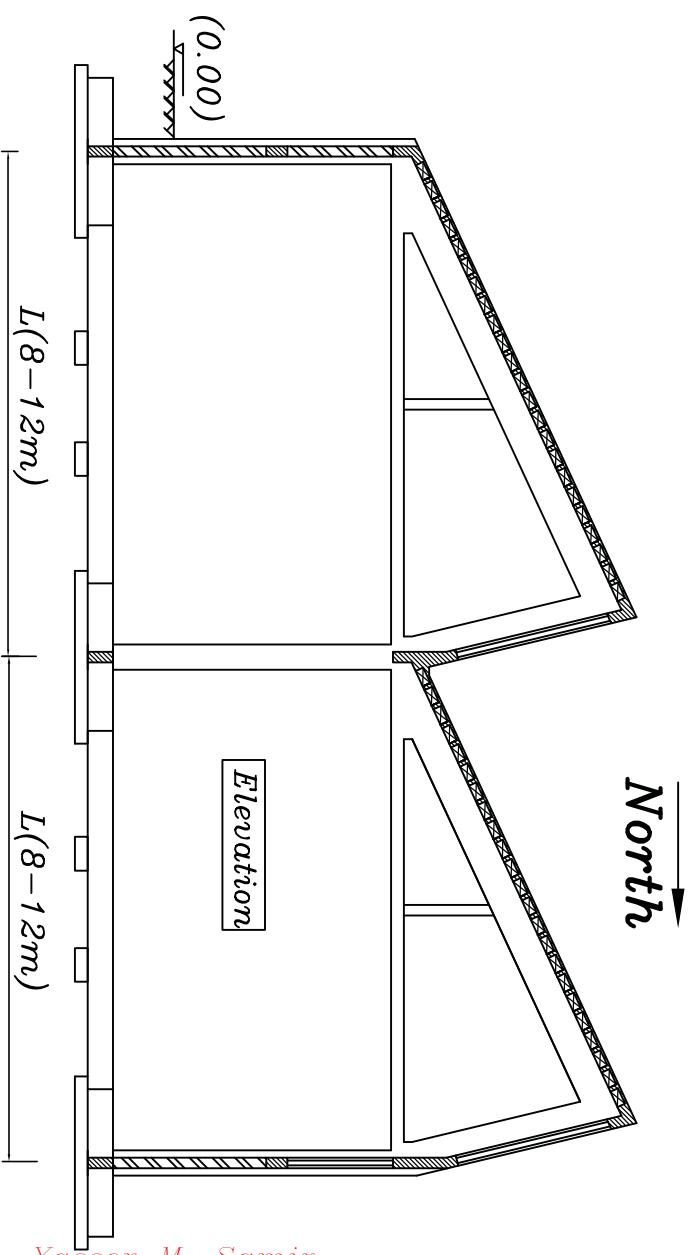
*Plan*



*Side view*

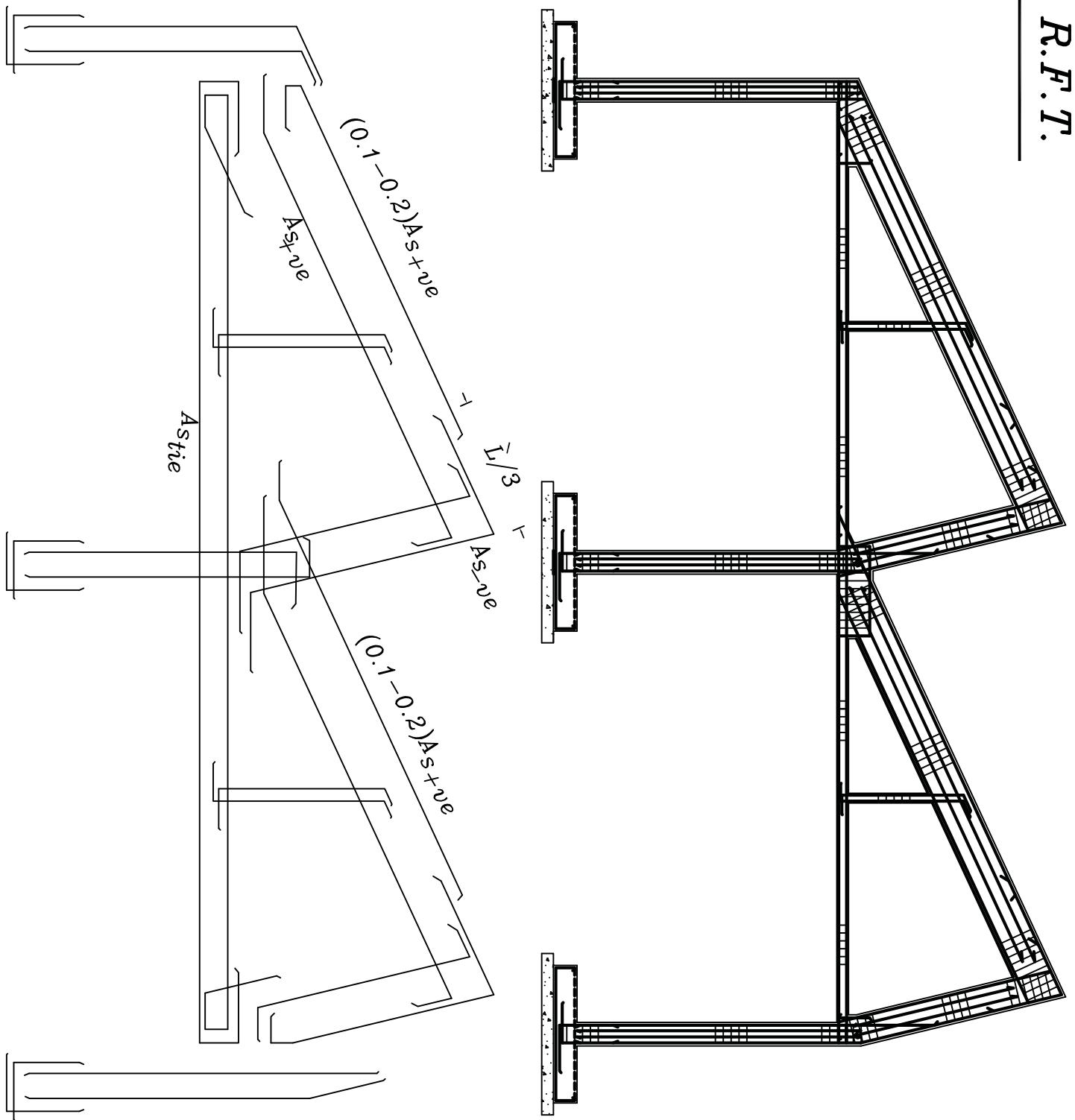


*Elevation*



North

## Details of R.F.T.



### Example(3)

North

For the given plan and cross-section,  
it is required to:

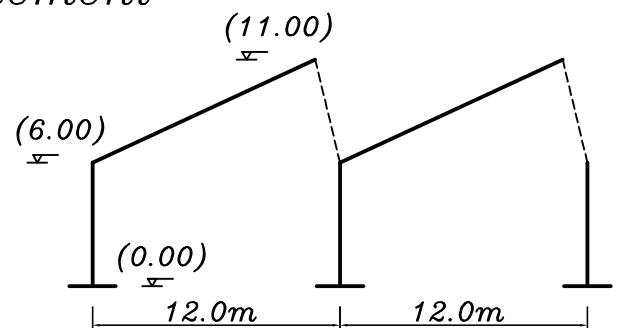
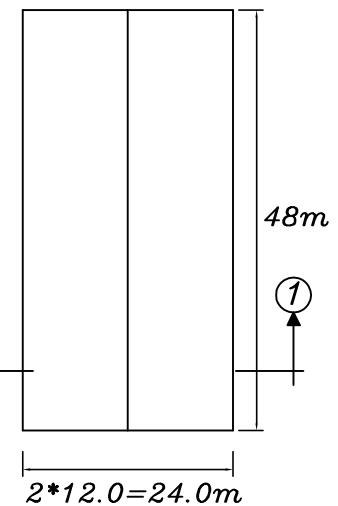
1-Choose the suitable system to cover  
this Area.

2-Design all Slabs and draw plan of Rft.

3-Design the main supporting element  
and draw details of Rft.

$$F.C. = 1.4 \text{ kN/m}^2, L.L = 1.0 \text{ kN/m}^2$$

$$f_{cu} = 25 \text{ N/mm}^2, f_y = 360 \text{ N/mm}^2$$

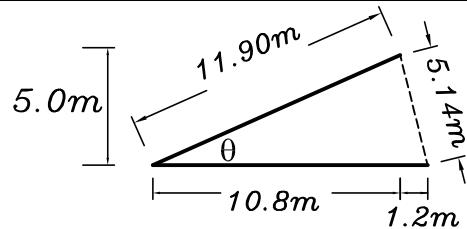


Sec. (1-1)

### Solution

$$t = \frac{600}{18} = 33.33 \text{ cm}$$

take  $t=25 \text{ cm}$  [20cm+5cm]  
check defl.



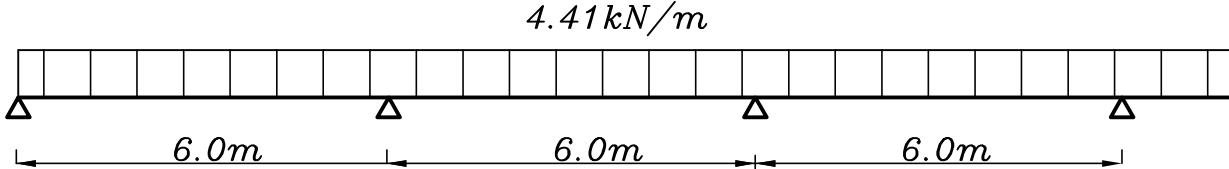
$$\theta = \tan^{-1} \left( \frac{5.0}{10.8} \right) = 24.84$$

$$w_{su} = \frac{1.4 [t s \delta_c * (e + b) + b h \delta_c + 5 * \text{wt. of block}]}{(e + b)} + 1.4 F.C. + 1.6 L.L. \cos \theta$$

$$w_{su} = \frac{1.4 [0.05 * 25 * 0.5 + 0.1 * 0.2 * 25 + 5 * 0.16]}{0.50} + 1.4 * 1.4 + 1.6 * 1.0 * 0.91$$

$$= 8.81 \text{ kN/m}^2$$

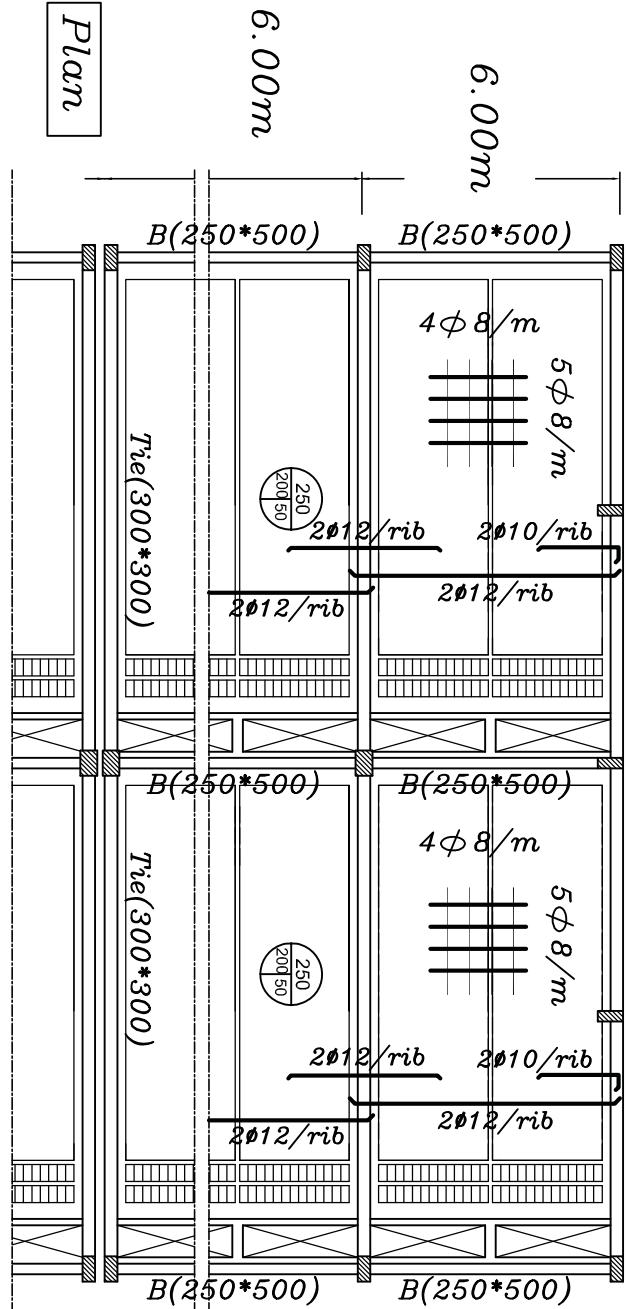
$$w_{su/Rib} = 0.5 * 8.81 = 4.41 \text{ kN/m}$$



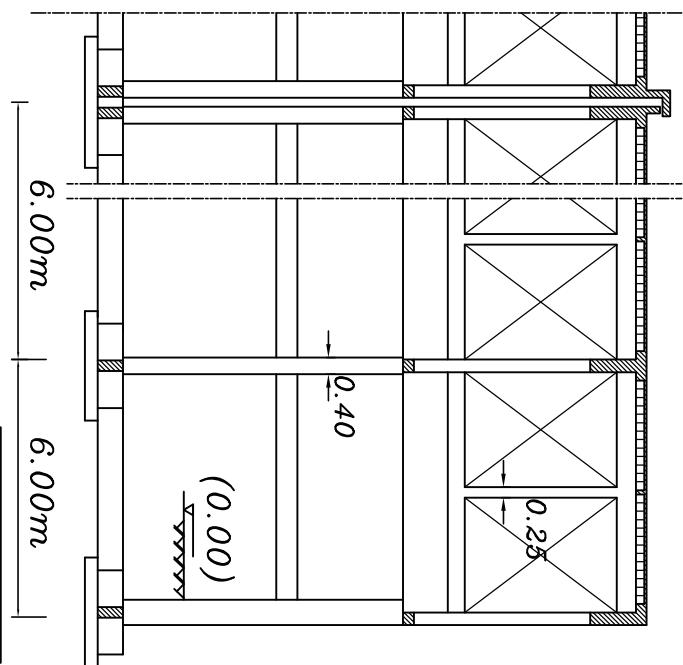
1:200—1:400

*KEY PLAN*

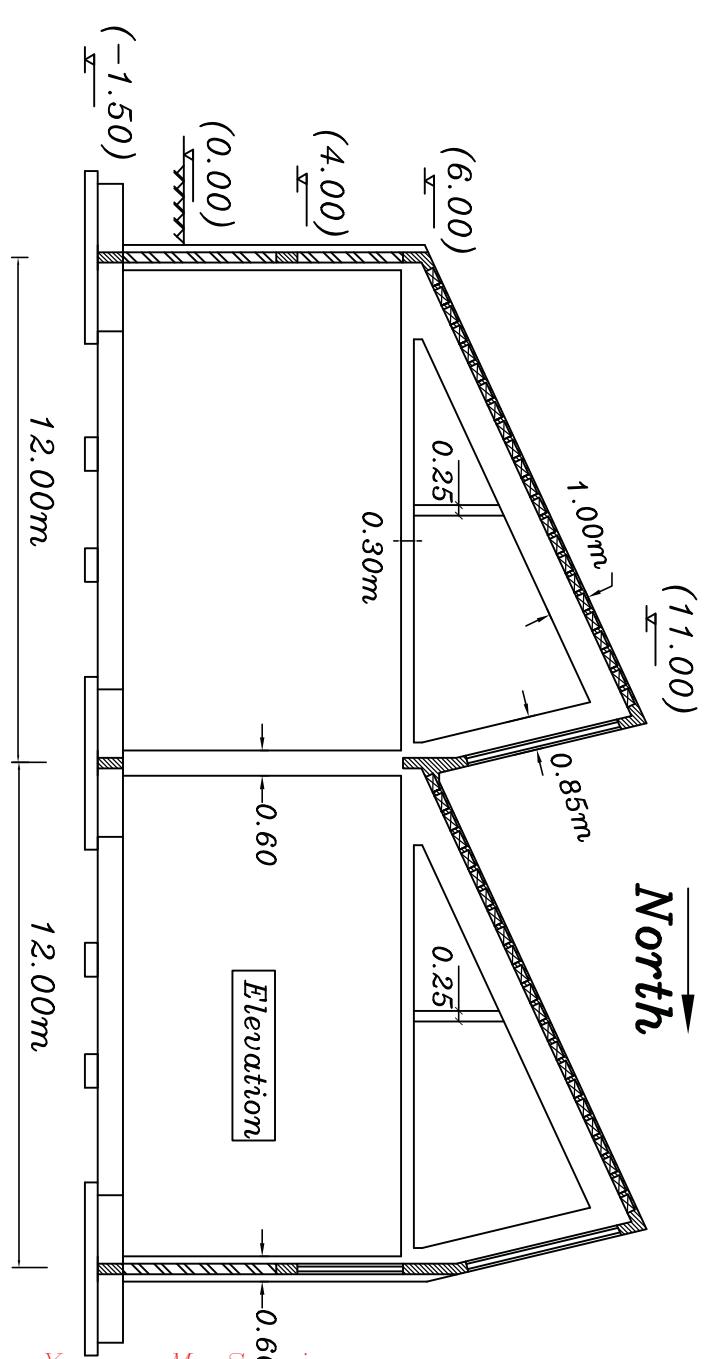
*Plan*

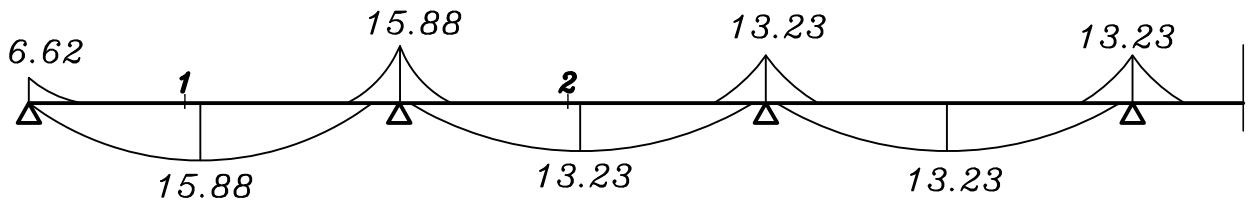


*Side view*



*Elevation*





### Sec. (1-1)

$$M_{des.} = M \cos \theta = 15.88 * 0.91 = 14.45 \text{ kN.m}$$

$$220 = C_1 \sqrt{\frac{14.45 * 10^6}{500 * 25}} \quad C_1 = 6.47 \quad J = 0.826$$

$$A_s = \frac{14.45 * 10^6}{0.826 * 360 * 220} = 221 \text{ mm}^2 / \text{rib}$$

$$A_s = 2 \phi 12 / \text{rib}$$

### Sec. (2-2)

$$M_{des.} = M \cos \theta = 13.23 * 0.91 = 12.04 \text{ kN.m}$$

$$220 = C_1 \sqrt{\frac{12.04 * 10^6}{500 * 25}} \quad C_1 = 7.09 \quad J = 0.826$$

$$A_s = \frac{12.04 * 10^6}{0.826 * 360 * 220} = 184 \text{ mm}^2 / \text{rib}$$

$$A_s = 2 \phi 12 / \text{rib}$$

### Analysis of Main System

$$w_1 = o.w. + w_{su} * \text{spacing}$$

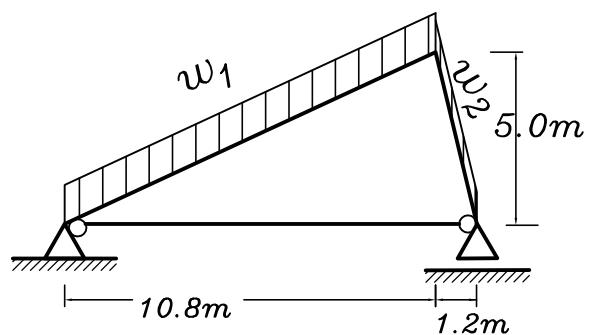
$$w_1 = 0.30 * 1.0 * 25 * 1.4 + 8.81 * 6.0$$

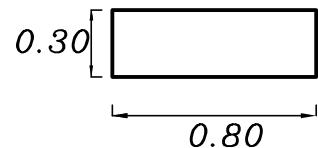
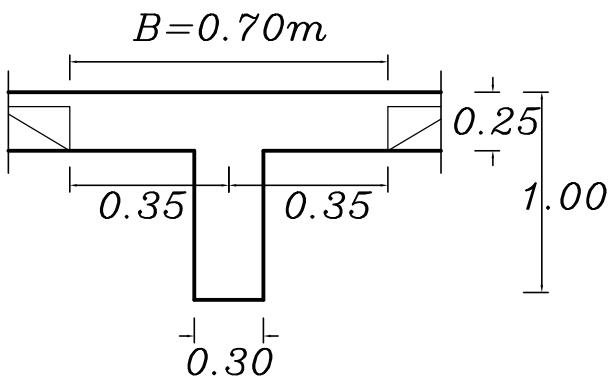
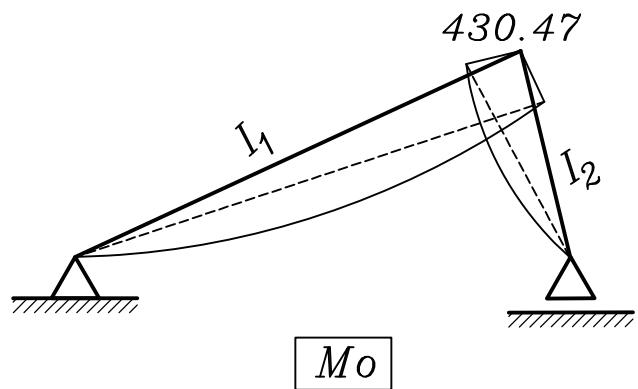
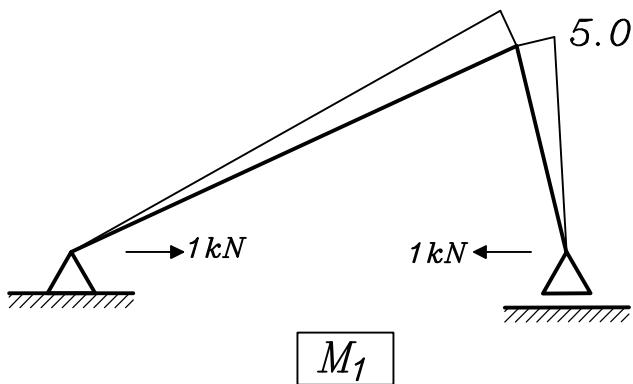
$$w_1 = 63.36 \text{ kN/m}$$

$$w_2 = o.w.$$

$$w_2 = 0.30 * 0.8 * 25 * 1.4$$

$$w_2 = 8.40 \text{ kN/m}$$





$$I_1 = 515 \cdot 10^{-4} \cdot 0.70 \cdot 1.0^3$$

$$I_1 = 0.036 m^4$$

$$I_2 = \frac{0.30 \cdot 0.80^3}{12}$$

$$I_2 = 0.013 m^4$$

$$\delta_{10} = -\frac{1}{3} \cdot \frac{11.90}{E_c I_1} [430.47 \cdot 5.0] - \frac{2}{3} \cdot \frac{11.90}{E_c I_1} \left[ \frac{63.36 \cdot 11.9 \cdot 10.8}{8} \cdot 2.5 \right]$$

$$-\frac{1}{3} \cdot \frac{5.14}{E_c I_2} [430.47 \cdot 5.0] - \frac{2}{3} \cdot \frac{5.14}{E_c I_2} \left[ \frac{8.4 \cdot 5.14 \cdot 1.20}{8} \cdot 2.5 \right]$$

$$\delta_{10} = \frac{-1085869.16}{E_c}$$

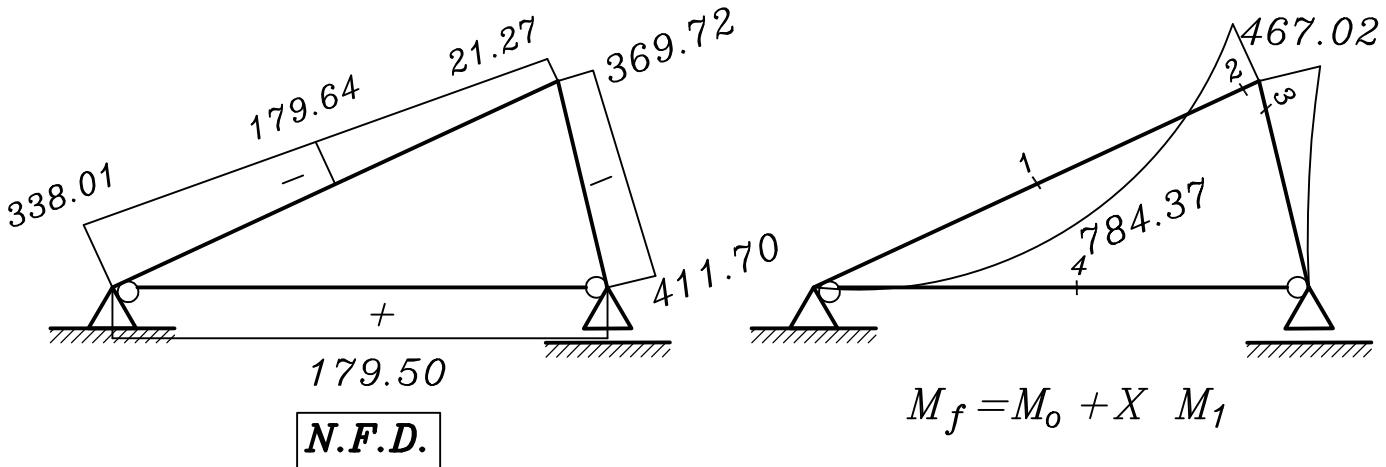
$$\delta_{11} = \frac{1}{3} \cdot \frac{11.90}{E_c I_1} [5.0^2] + \frac{1}{3} \cdot \frac{5.14}{E_c I_2} [5^2]$$

$$\delta_{11} = \frac{6049.50}{E_c}$$

$$\delta_{10} + x \delta_{11} = 0$$

$$-\frac{1085869.16}{E_c} + \frac{6049.50}{E_c} X = 0$$

$$X = 179.50 kN$$



Sec(1-1)

$$\frac{N_{u.l.}}{b t f_{cu}} = \frac{179.64 * 10^3}{300 * 1000 * 25} = 0.02 < 0.04 \text{ (neglect } N)$$

$$950 = C_1 \sqrt{\frac{784.37 * 10^6}{700 * 25}} \quad C_1 = 4.49 \quad J = 0.818$$

$$A_s = \frac{784.37 * 10^6}{0.818 * 950 * 360} = 2804 \text{ mm}^2$$

$$A_s = 8 \phi 22$$

Sec(2-2)

$$950 = C_1 \sqrt{\frac{467.02 * 10^6}{300 * 25}} \quad C_1 = 3.81 \quad J = 0.796$$

$$A_s = \frac{467.02 * 10^6}{0.796 * 950 * 360} = 1716 \text{ mm}^2$$

$$A_s = 5 \phi 22$$

Sec(3-3)

$$\frac{N_{u.l.}}{b t f_{cu}} = \frac{369.72 * 10^3}{300 * 800 * 25} = 0.062 > 0.04 \text{ (Don't neglect } N)$$

$$e = \frac{M_{u.l.}}{N_{u.l.}} = \frac{467.02}{369.72} = 1.26 \text{ m}$$

$$\frac{e}{t} = \frac{1.26}{0.80} = 1.58 > 0.5 \text{ (big eccentricity)}$$

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$$e_s = e + \frac{t}{2} - c = 1.26 + \frac{0.80}{2} - 0.05 = 1.61 \text{ m}$$

$$M_{us} = N_{u.l.} * e_s = 369.72 * 1.61 = 595.25 \text{ kN.m}$$

$$750 = C_1 \sqrt{\frac{595.25 * 10^6}{300 * 25}} \quad C_1 = 2.66 < 2.78$$

$$\text{assume } t = 0.85 \text{ m} \quad 800 = C_1 \sqrt{\frac{595.25 * 10^6}{300 * 25}} \quad C_1 = 2.84 \& J = 0.72$$

$$A_s = \frac{595.25 * 10^6}{0.72 * 800 * 360} - \frac{369.72 * 10^3}{360 / 1.15} = 1672 \text{ mm}^2$$

$$A_s = 5 \phi 22$$

### Sec(4-4)

$$A_s = \frac{179.50 * 10^3}{360 / 1.15} = 5.73 \text{ cm}^2 = 6 \phi 12$$

### 8] Design of Inner Col. (400\*600)

$$P_{col.} = 797.16 \text{ kN}$$

$$\delta_{b_{in}} = \frac{1.2 * 6.75}{0.60} = 13.50 \quad \delta_{b_{out}} = \frac{1.2 * 6.25}{0.40} = 18.75$$

Column is long col. inside & outside plan

$$\delta_b = \frac{\delta_b^2 b}{2000} = \frac{18.75^2 * 0.40}{2000} = 0.07 \text{ m}$$

$$M_{add} = 797.16 * 0.07 = 56.05 \text{ kN.m}$$

$$\frac{N_{u.l.}}{bt f_{cu}} = \frac{797.16 * 10^3}{400 * 600 * 25} = 0.13 \quad \zeta = \frac{400 - 100}{400} = 0.75$$

$$\frac{M_{u.l.}}{bt^2 f_{cu}} = \frac{56.05 * 10^6}{600 * 400^2 * 25} = 0.023$$

$\rho < 1$  Take  $\rho = 1$

$$A_{S \ min} = \frac{0.25 + 0.052 * 18.75}{100} * 400 * 600 = 2940 \text{ mm}^2$$

$A_s = 12 \phi 18$  *By Eng. Ezz El-Din Mostafa & Eng. Yasser M. Samir*

# Details of R.F.T.

